# Conformations of Stilbene-like Species and New Method of Energy Partition 

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#### Abstract

To understand the nature of $\pi$-electron delocalization, while questioning the abnormally large twist angle of $N$-benzylideneaniline, we prepared four stilbene-like species, (4-X-Ph)-CH=N-Ar (Ar $=2-$ pyridyl, $\mathrm{X}=-\mathrm{Cl}$, $-\mathrm{NO}_{2},-\mathrm{N}(\mathrm{Me})_{2}$; $\mathrm{Ar}=2$-pyrimidyl, $\left.\mathrm{X}=-\mathrm{NO}_{2}\right)$, and four ketenimine derivatives, $(4-\mathrm{X}-\mathrm{Ph})_{2} \mathrm{C}=\mathrm{C}=\mathrm{N}-(\mathrm{Ph}-\mathrm{Y}-4)$ ( $\left.\mathrm{Y}=-\mathrm{H}, \mathrm{X}=-\mathrm{H} ; \mathrm{Y}=-\mathrm{NO}_{2}, \mathrm{X}=-\mathrm{H} ; \mathrm{Y}=-\mathrm{NO}_{2}, \mathrm{X}=-\mathrm{OMe} ; \mathrm{Y}=-\mathrm{N}(\mathrm{Me})_{2}, \mathrm{X}=-\mathrm{H}\right)$, and determined their crystal structures using X-ray diffraction. Our new procedure for constructing a complete fragment molecular orbital (FMO) basis set is described in detail. Based on our procedure, the Morokuma's energy partitioning provides, in the framework of ab initio SCF-MO computation at the STO-3G level, the various $\pi$ and $\sigma$ energies associated with the inter- and intrafragment interactions. The $\pi$-electron delocalization in the DPI state of stilbene-like species is found to be destabilization. The DPI state is most destabilized at the coplanar geometry, and its electronic energy is the highest of four hypothetical electronic states. The characteristics of the quantum mechanical resonance energy (QMRE), including its role with regard to chemical reactivities toward electrophile attack, depend upon the response of the $\sigma$ framework to the $\pi$-electron delocalization. In the case of stilbene-like species, the QMRE is destabilizing. Conversely, the QMRE of benzene is stabilizing. However, it is the $\sigma$ framework of benzene, rather than the $\pi$ system itself, which is strongly stabilized by the QMRE, revealing that benzene is $\sigma$ aromatic. The driving forces for the out-of-plane twist of stilbene-like species arise from the QMRE and the $\sigma$ orbital interaction. The electron-withdrawing ( -I ) groups and the ring-nitrogen atoms seem to have an obvious influence upon the twist angle.


## Introduction

It has been recognized as a cornerstone of the classical structure theory of organic chemistry that molecules with conjugated double bonds have a higher thermodynamic stability than isomeric compounds having isolated double bonds. The standard textbook explanation for this stability is given in terms of resonance interactions. ${ }^{1}$ It is also one of the fundamental concepts that the maximum resonance energy results from the planarity of the $\pi$ system. ${ }^{1,2}$ However, the abnormally large twist angle of stilbene-like species seems to challenge the viewpoint of $\pi$ resonance stabilization.

The marked dissimilarity in the electronic spectra of stilbene (STB, 1a) and $N$-benzylideneaniline (NBA) has led to many theoretical and experimental studies and arguments in the past two or three decades, including studies employing infrared (IR) and a variety of nuclear magnetic resonance (NMR) studies, X-ray crystallography, and molecular orbital calculations. ${ }^{3}$ The resonance stabilization is always used to interpret the effects of substituents on the conformations of NBA and its substituted derivatives. ${ }^{4}$ Burgi and recent researchers ascribed the large twist angle ( $\phi=55^{\circ}$ ) of NBA to the contact of nonbonded atoms such as the hydrogen on the $-\mathrm{N}=\mathrm{CH}$ - and one of the ortho hydrogens on the aniline ring. The loss of the $\pi$-electron energy in the twisted geometry can be compensated for partly by the intramolecular charge transfer (CT-2) from the bridge nitrogen lone-pair electrons to the phenyl ring and by the decrease in steric hindrance; ${ }^{5}$ these researchers expected, therefore, that if the nonbonded interaction was neglected, the $\pi$-electron transfer (CT-1) between the conjugated fragments was found to favor the planar conformation of NBA. ${ }^{6}$ Burgi's conclusions appear

[^0]to be questioned by the angles $\phi$ of stilbene-like species, especially by those (both up to $30^{\circ}$ ) of $\mathbf{1 a}$ and azobenzene ( $\mathbf{1 d}$ ) in the gas state, ${ }^{7}$ and by those of the compounds listed in Table 1. (The phrase "stilbene-like species listed in Table 1 " or "the molecules of type $\mathbf{1}$ " is often, hereafter, shortened to "STBtype $1 "$.)
In order to discern whether conjugation effect depends on conformation or results in a nonplanar geometry, we prepared the following eight compounds with less nonbonded contact such as that in NBA: (4-X-Ph)-CH=N-2-pyridyl $(\mathbf{1 e}, \mathrm{X}=-\mathrm{Cl}$; 1f, $\left.\mathrm{X}=-\mathrm{NO}_{2} ; \mathbf{1 g}, \mathrm{X}=(\mathrm{Me})_{2} \mathrm{~N}-\right), 4-\mathrm{NO}_{2}-\mathrm{Ph}-\mathrm{CH}=\mathrm{N}-2-$ pyrimidyl (1i) and (4-X-Ph) ${ }_{2} \mathrm{C}=\mathrm{C}=\mathrm{N}-(\mathrm{Ph}-\mathrm{Y}-4)(\mathbf{2 a}, \mathrm{X}=-\mathrm{H}$, $\mathrm{Y}=-\mathrm{H} ; \mathbf{2 b}, \mathrm{X}=-\mathrm{H}, \mathrm{Y}=-\mathrm{NO}_{2} ; \mathbf{2 c}, \mathrm{X}=-\mathrm{MeO}, \mathrm{Y}=-\mathrm{NO}_{2}$; 2d, $\left.\mathrm{X}=-\mathrm{H}, \mathrm{Y}=-\mathrm{N}(\mathrm{Me})_{2}\right)$ and determined their crystal structures using X-ray diffraction (see Table 1 and Figures 1-3).
The total molecular energies $E^{\mathrm{T}}$, total electronic energies $E_{\mathrm{e}}$, and total nuclear repulsion energies $E_{\mathrm{N}}$, occurring in seven typical optimized geometries of each of seven STB-type 1 were calculated using the AM1 method. ${ }^{12}$ In addition, the nuclear repulsion energies $E_{\mathrm{n}}$ between the aromatic ring and fragment Ar-Q $=\mathrm{P}$ - were obtained from the ab initio SCF-MO (selfconsistent field molecular orbital) program. The nonbonded contact in $\mathbf{1 e} \mathbf{- 1 g}$ and $\mathbf{1 i}$ (Figure 1) should be comparable to that in 2a-2d (Figure 2), but the twist angles $\phi$ for the former are generally larger than those for the latter. Of all the molecules listed in Table 1, the theoretical angle ( $\phi=50^{\circ}$ ) of $1 \mathbf{i}$ is largest and the experimental angle ( $\phi=0.5^{\circ}$ ) of $\mathbf{2 a}$ is smallest. The data in Table 2 are especially noteworthy. These data show identically that the driving force for out-of-plane twist of STB-type 1 arises from the electron interaction, expressed in terms of $E_{\mathrm{e}}$, rather than from the nuclear repulsion $E_{\mathrm{N}}$ and $E_{\mathrm{n}}$. At the $\theta=30^{\circ}$ geometry of $\mathbf{1 h}$, for example, the absolute

TABLE 1: Experimental and Theoretical Values (deg) of Twist Angles $\phi$ and $\alpha$ in Compounds of Types 1 and 2

|  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  | twist angle $\phi$ |  | twist angle $\alpha$ |  |
| compd | P | Q | X | Y | Z | W | R | $\mathrm{R}^{\prime}$ | X-ray | AM1 | X-ray | AM1 |
| 1a | CH | CH | CH | CH | CH | C | H | H | $5{ }^{a}$ | 27 | 5 | 27 |
| 1b | N | CH | CH | CH | CH | C | $\mathrm{N}(\mathrm{Me})_{2}$ | $\mathrm{NO}_{2}$ | $41^{\text {b }}$ | 40 | 10 | 0 |
| 1c | N | CH | CH | CH | CH | C | $\mathrm{NO}_{2}$ | $\mathrm{N}(\mathrm{Me})_{2}$ | $9^{\text {b }}$ | $15^{e}$ | 4 | 0 |
| 1d | N | N | CH | CH | CH | C | H | H | $15^{\text {c }}$ | 15 | 15 | 15 |
| 1e | N | CH | N | CH | CH | C | Cl | H | 15 | 13 | 6 | 3 |
| 1 f | N | CH | N | CH | CH | C | $\mathrm{NO}_{2}$ | H | 20 | 0 | 2 | 0.5 |
| 1 g | N | CH | N | CH | CH | C | $\mathrm{N}(\mathrm{Me})_{2}$ | H | 36 | $15^{e}$ | 7 | 0 |
| 1h | N | CH | CH | CH | N | C | $\mathrm{H}$ | H | $46^{d}$ | 38 | 13.4 | 14 |
| 1 i | N | CH | N | N | $\mathrm{CH}$ | C | $\mathrm{NO}_{2}$ | $\mathrm{H}$ | $26$ | $50$ | 12 | 4.5 |
| 1j | N | CH | CH | CH | CH | N |  | H | $21^{d}$ | $35^{e}$ | 8 | 2 |
| 2 a |  |  |  |  |  |  | H | H | 0.5 |  |  |  |
| 2b |  |  |  |  |  |  | $\mathrm{NO}_{2}$ | H | 16 |  |  |  |
| 2c |  |  |  |  |  |  | $\mathrm{NO}_{2}$ | MeO | 6.5 |  |  |  |
| 2d |  |  |  |  |  |  | $\mathrm{N}(\mathrm{Me})_{2}$ | H | 9.1 |  |  |  |

${ }^{a}$ This value is from ref $8 .{ }^{b}$ From ref $9 .{ }^{c}$ From ref $10 .{ }^{d}$ From ref $11 .{ }^{e}$ Conformational space was sampled by varying $\theta$ in steps of $5{ }^{\circ}$.
value (|-11 $090.9611 \mid \mathrm{eV}$ ) of $E_{\mathrm{e}}$ and value ( 9004.6837 eV ) of $E_{\mathrm{N}}$ are greatest, and decrease as the molecular framework is distorted away from this geometry. Therefore, we cannot attribute the nonplanarity of STB-type 1 to the steric hindrance or to the crystal lattice force. ${ }^{13}$ In molecule 2c (Figure 2), the combination of the "pushing" and "pulling" actions, exerted by an electron-releasing ( +M ) group $\mathrm{MeO}-$ and an electronwithdrawing $(-\mathrm{M})$ group $-\mathrm{NO}_{2}$, respectively, should greatly benefit the CT- 2 interaction between the nitrogen lone pair and phenyl ring $A$, and its twist angle $\mathrm{C}_{8}-\mathrm{N}_{7}-\mathrm{C}_{1}-\mathrm{C}_{6}$ should be larger than the angle $\left(41^{\circ}\right)$ in $\mathbf{1 b}$. At the least, it should be larger than that $\left(16^{\circ}\right)$ in $\mathbf{2 b}$. Contrary to expectation, the actual angle is only $9.2^{\circ}$. Nakai and collaborators found that the $\mathrm{C}_{1}-$ $\mathrm{N}_{7}$ distance in several molecules such as $\mathbf{1 c}(1.416 \AA$ ) and $\mathbf{1 b}$ $(1.398 \AA)$ decreases with increasing CT-2 effect. ${ }^{9}$ Accordingly, this distance should decrease in order of $\mathbf{1 f}, \mathbf{1 i}$, and $\mathbf{1 g}$ and of $\mathbf{2 d}, \mathbf{2 a}, \mathbf{2 b}$, and $\mathbf{2 c}$, respectively. In fact, the bond length (1.439 $\AA$ ) in $\mathbf{1 i}$ is much longer than that ( $1.410 \AA$ ) in $\mathbf{1 f}$, and the experimental value ( $1.409 \AA$ ) in $\mathbf{1 g}$ is almost equal to that in $\mathbf{1 f}$ (Figure 1); of the four ketenimine derivatives, the distance (1.436 $\AA$ ) in 2a is longest and that $(1.419 \AA$ ) in $\mathbf{2 d}$ is shortest (Figure 2). Recently, our calculations have approximately shown that in the aniline molecule, the CT-2 interaction is destabilizing. ${ }^{14}$ Accordingly, the nonplanarity of STB-type 1 cannot be explained in terms of the CT-2.

In this work, our procedure for constructing a complete fragment molecular orbital (FMO) basis set is described in detail. Morokuma's partition of the intermolecular SCF interaction energy, ${ }^{15}$ denoted as M-SCF partition, is introduced into the intramolecular interaction, and it is used for analyzing the direct and indirect effects of the $\pi$-electron delocalization, respectively, on the $\pi$ system itself and the $\sigma$ frame in an effort to gain insight into the nature of the $\pi$-electron delocalization. Meanwhile, it is also applied to the $\sigma$ interactions in order to search for the unknown driving force and to probe the influence of the electron-withdrawing ( -I ) effect upon the twist angle.

## Methods and Computational Details

Based on the most common definitions of the resonance energy (RE), ${ }^{16}$ the RE is essentially associated with the local interaction between double bonds. Inevitably, this interaction influences the original characteristics of the double bonds, including the observed and calculable changes in their bond lengths and bond orders, and also including the disturbance to their original $\pi$ energies. ${ }^{17}$ The geometric data in Figure 3, for example, indicate that the lengths of the bonds $\mathrm{N}_{7}-\mathrm{C}_{8}$ and $\mathrm{C}_{1}-$ $\mathrm{C}_{6}$ are changed as the bond $\mathrm{C}_{1}-\mathrm{N}_{7}$ is lengthened from 1.405 to $1.411 \AA$ with the rotation of fragment A about the $\mathrm{C}_{1}-\mathrm{N}_{7}$. Accordingly, the fundamental problems in the energy partitioning are how to calculate, reasonably and directly, the $\pi$ energies occurring in a conjugated molecule and its corresponding hypothetical structures with the localized $\pi$ systems, and how to evaluate the effects of the $\pi$-electron delocalization on the $\sigma$ framework. In this sense, the perturbation molecular orbital (PMO) method should be more reasonable and valuable. It is prerequisite for the PMO analysis that the symmetric ( $\sigma$ ) and antisymmetric ( $\pi$ ) FMOs are thoroughly separated. It is easy when and only when the geometry of a molecule is planar. ${ }^{18}$ However, STB-type $\mathbf{1}$ are not planar. In this case, the M-SCF method based on our new procedure becomes a useful instrument for partitioning total electronic energy. Our procedure provides a complete FMO basis set for the M-SCF partition.

According to the PMO theory ${ }^{19}$ and based on the fact that in STB-type 1 both twist angles $\phi$ and $\alpha$ are not equal to $0^{\circ}$ or $180^{\circ}$, we can consider a nonplanar molecule $N$-phenylmethyl-ene-3-pyridineamine ( $\mathbf{1 h}$ ), for example, as three planar openedshell fragments, phenyl fragment (A), imine group $-\mathrm{CH}=\mathrm{N}-(\mathrm{B})$, and 3-pyridyl fragment (C), i.e., $\mathrm{A}-\mathrm{B}-\mathrm{C}$ dissection as shown in Figure 4.

Figure 5 displays a thermodynamic cycle for the orbital interactions in STB-type 1. It shows the symbols for the $\pi$ and $\sigma$-electronic energies in the following hypothetical states: the full localized state denoted as FUL; the state, denoted as DPI, with a delocalized $\pi$ system and localized $\sigma$ frameworks;

$\begin{array}{ll}\mathrm{CB}-\mathrm{N} 7-\mathrm{C} 1-\mathrm{N} 6=-15.6 & \mathrm{~N} 7-\mathrm{C8}-\mathrm{C} 9-\mathrm{C} 14= \\ \mathrm{C} 5-\mathrm{N} 6-\mathrm{C} 1-\mathrm{N} 7=-179.8 & \mathrm{CB}-\mathrm{C} 9-\mathrm{C} 10-\mathrm{C} 11=178.9\end{array}$

$\mathrm{C} 8-\mathrm{N} 7-\mathrm{C} 1-\mathrm{N} 6=-19.6 \quad \mathrm{~N} 7-\mathrm{C} 8-\mathrm{C} 9-\mathrm{C} 14=-1.9$
$\mathrm{C} 5-\mathrm{N} 6-\mathrm{C} 1-\mathrm{N} 7=177.3 \quad \mathrm{C} 8-\mathrm{C} 9-\mathrm{C} 10-\mathrm{C} 11=-179.2$


C8-N7-C1-N6 $=35.6 \quad \mathrm{~N} 7-\mathrm{CB}-\mathrm{C} 9-\mathrm{C} 14=7.0$
$\mathrm{C} 5-\mathrm{N} 6-\mathrm{C} 1-\mathrm{N} 7=179.0 \quad \mathrm{C}-\mathrm{C} 9-\mathrm{C} 10-\mathrm{C} 11=179.6$


## Crystal Structures



C8-N7-C1-N6 $=-13.6 \quad$ N7-C8-C9-C14 $=2.9$ C5-N6-C1-N7 $=-178.4 \quad$ C8-C9-C10-C11 $=179.8$



$\mathrm{C} 8-\mathrm{N} 7-\mathrm{C} 1-\mathrm{N} 6=-50.0 \quad \mathrm{~N} 7-\mathrm{C} 8-\mathrm{C} 9-\mathrm{C} 14=4.5$
C5-N6-C1-N7=-175.0 C8-C9-C10-C11= 179.9

## Preferential Geometries Obtained from AM1

Figure 1. Experimental and theoretical geometric data of four stilbene-like molecules.
the DSI state with delocalized $\sigma$ frameworks and localized $\pi$ systems; the full delocalized state denoted as FUD. Figure 5 also contains a set of definitions of the various energy differences that will be used consistently in this work. For simplicity, these energy differences are expressed by the following general formulas:

$$
\begin{align*}
& \Delta E_{\pi}^{(\lambda, \rho)}=\Delta E_{a b+b c+c a}^{(\lambda, \rho)-\pi}+\Delta E_{a+b+c}^{(\lambda, \rho)-\pi}  \tag{1-1}\\
& \Delta E_{\sigma}^{(\lambda, \rho)}=\Delta E_{a b+b c+c a}^{(\lambda, \rho)-\sigma}+\Delta E_{a+b+c}^{(\lambda, \rho)-\sigma} \tag{1-2}
\end{align*}
$$

where the characters $\lambda$ and $\rho(\lambda, \rho=\pi, \sigma)$ in the superscript
( $\lambda, \rho$ ) mean that the energy effects $\Delta E_{\pi}^{(\lambda, \rho)}$ and $\Delta E_{\sigma}^{(\lambda, \rho)}$ arise from the delocalization of the $\lambda$ - and $\rho$-electrons; the characters $\pi$ and $\sigma$ in super- and subscripts denote that the energy effects are associated, respectively, with the $\pi$ and $\sigma$ orbital interactions. When $\lambda=\pi$ and $\rho=\pi$, eqs (1-1) and (1-2) become

$$
\begin{align*}
& \Delta E_{\pi}^{(\pi)}=\Delta E_{a b+b c+c a}^{(\pi)-\pi}+\Delta E_{a+b+c}^{(\pi)-\pi}  \tag{2-1}\\
& \Delta E_{\sigma}^{(\pi)}=\Delta E_{a b+b c+c a}^{(\pi)-\sigma}+\Delta E_{a+b+c}^{(\pi)-\sigma} \tag{2-2}
\end{align*}
$$

where $\Delta E_{\pi}^{(\pi)}$ and $\Delta E_{\sigma}^{(\pi)}$ are the energy differences between the DPI and FUL states. Two terms in the right side of eq (2-1)


Figure 2. Crystallographic data of four ketenimine derivatives.
are the energy components associated, respectively, with the inter- and intrafragment interactions, and are given as

$$
\begin{gather*}
\Delta E_{a b+b c+c b}^{(\pi)-\pi}=\Delta E_{a b}^{(\pi)-\pi}+\Delta E_{b c}^{(\pi)-\pi}+\Delta E_{c a}^{(\pi)-\pi}  \tag{2-3}\\
\Delta E_{a+b+c}^{(\pi)-\pi}=\Delta E_{a}^{(\pi)-\pi}+\Delta E_{b}^{(\pi)-\pi}+\Delta E_{c}^{(\pi)-\pi} \tag{2-4}
\end{gather*}
$$

where

$$
\begin{array}{r}
\Delta E_{a}^{(\pi)}=E_{a}^{(\pi)-\pi}-E_{a}^{(0)-\pi}, \Delta E_{b}^{(\pi)}=E_{b}^{(\pi)-\pi}-E_{b}^{(0)-\pi}, \Delta E_{c}^{(\pi)}= \\
E_{c}^{(\pi)-\pi}-E_{c}^{(0)-\pi}(2-5 \tag{2-5}
\end{array}
$$

In the case of STB-type $\mathbf{1},\left|\Delta E_{a c}^{(\pi)-\pi}\right|<10^{-3}$; hence, eq (2-3) is
often written as

$$
\begin{equation*}
\Delta E_{a b+b c}^{(\pi)-\pi}=\Delta E_{a b}^{(\pi)-\pi}+\Delta E_{b c}^{(\pi)-\pi} \tag{2-6}
\end{equation*}
$$

In this work, the energy components such as those in eqs (2-3)-(2-6) are often written as the general forms $\Delta E_{p q}^{(\pi)-\lambda}$ and $\Delta E_{p}^{(\pi)-\lambda}$ where $\left.p, q=a, b, c ; p \neq q ; \lambda=\pi, \sigma\right)$. In this case, the subscript $p q$ and the character $\lambda$ in the superscript $(\pi)-\lambda$ mean that the $\Delta E_{p q}^{(\pi)-\lambda}$ is associated with the $\lambda$ orbital interactions between fragment P and $\mathrm{Q}(\mathrm{P}, \mathrm{Q}=\mathrm{A}, \mathrm{B}, \mathrm{C} ; \mathrm{P} \neq \mathrm{Q})$, and the subscript $p$ denotes a energy effect $\Delta E_{p}^{(\pi)-\lambda}$ occurring in fragment P . In eq (2-5), the character o in the superscript (o) denotes that the $E_{p}^{(0)-\lambda}(p=a, b, c ; \lambda=\pi, \sigma)$ is a $\lambda$ electronic

TABLE 2: Total Molecular Energy $E^{\text {T }}$, Total Electronic Energy $E_{\mathrm{e}}$, Total Nuclear Repulsion $\boldsymbol{E}_{\mathrm{N}}$, Nuclear Repulsion $E_{\mathrm{n}}$ (hartrees) between Fragments $\mathbf{C}$ and $\mathbf{A}+\mathbf{B}$, and Their Changes with Rotation of Fragment $\mathbf{C}$ (Energy in eV except for $\left.\boldsymbol{E}_{\mathbf{n}}\right)^{a}$

|  | $\theta=0^{\circ}$ | $\theta=5^{\circ}$ | $\theta=10^{\circ}$ | $\theta=30^{\circ}$ | $\theta=50^{\circ}$ | $\theta=70^{\circ}$ | $\theta=90^{\circ}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | 1a |  |  |  |
| $E^{\text {T }}$ | -1956.3956 | -1956.3965 | -1956.3988 | -1956.4010 | -1956.3544 |  |  |
| $E_{\text {e }}$ | -10866.6455 | -10867.0250 | -10868.0638 | -10874.0003 | -10871.0929 |  |  |
| $E_{\mathrm{N}}$ | 8910.2499 | 8910.6289 | 8911.6649 | 8917.5993 | 8914.7384 |  |  |
| $E_{\mathrm{n}}$ | 229.3696 | 229.3942 | 229.4682 | 229.9104 | 229.8220 |  |  |
| 1b |  |  |  |  |  |  |  |
| $E^{\text {T }}$ | -3 383.8153 | -3 383.8150 | -3 383.8191 | -3 383.8376 | -3 383.8378 | -3 383.8211 |  |
| $E_{\text {e }}$ | -20 354.9945 | -20 355.6694 | -20 356.3679 | -20 362.3796 | -20 360.1906 | -20 351.4668 |  |
| $E_{\mathrm{N}}$ | 16971.1792 | 16971.8534 | 16972.5488 | 16978.5420 | 16976.3527 | 16967.6457 |  |
| $E_{\mathrm{n}}$ | 381.1377 | 381.1843 | 381.2470 | 381.7394 | 381.5754 | 380.8868 |  |
| 1d |  |  |  |  |  |  |  |
| $E^{\text {T }}$ | -2 085.5479 | -2 085.5481 | -2 085.5484 | -2 085.5425 | -2 085.5071 | -2 085.4587 | -2 085.4424 |
| $E_{\text {e }}$ | -11110.8509 | $-11110.8661$ | -11110.9009 | -11111.6857 | -11111.8174 | -11108.9611 | -11107.4265 |
| $E_{\mathrm{N}}$ | 9025.3029 | 9025.3181 | 9025.3525 | 9026.1432 | 9026.3103 | 9023.5024 | 9021.9545 |
| $E_{\mathrm{n}}$ | 237.0091 | 237.0092 | 237.0093 | 237.0371 | 237.0132 | 236.8095 | 236.6407 |
| 1e |  |  |  |  |  |  |  |
| $E^{\text {T }}$ | -2 446.2838 | -2 446.2839 | -2 446.2841 | -2 446.2803 | -2 446.2559 | -2 446.2068 |  |
| $E_{\text {e }}$ | -12559.3338 | -12559.3430 | -12559.5186 | -12560.4603 | -12560.3311 | -12557.6144 |  |
| $E_{\mathrm{N}}$ | 10113.0499 | 10113.0591 | 10113.2345 | 10114.1800 | 10114.0752 | 10111.4076 |  |
| $E_{\mathrm{n}}$ | 272.0361 | 272.0402 | 272.0553 | 272.1561 | 272.1461 | 271.8893 |  |
| $1 f$ |  |  |  |  |  |  |  |
| $E^{\text {T }}$ | -2917.0114 | -2 917.0114 | -2917.0113 | -2917.0062 | -2 916.9803 |  |  |
| $E_{\text {e }}$ | -15 549.8119 | -15549.8462 | -15549.9552 | -15551.1046 | -15551.0171 |  |  |
| $E_{\mathrm{N}}$ | 12632.8005 | 12632.8348 | 12632.9439 | 12634.0984 | 12634.0368 |  |  |
| $E_{\mathrm{n}}$ | 284.5411 | 284.5444 | 284.5526 | 284.6605 | 284.6523 |  |  |
| 1h |  |  |  |  |  |  |  |
| $E^{\text {T }}$ | -2 086.2632 | -2 086.2643 | -2 086.2665 | -2 086.2773 | 2086.2675 | -2 086.2417 | -2 086.2269 |
| $E_{\text {e }}$ | -11087.7973 | -11087.8483 | -11088.1340 | -11090.9611 | -11089.0204 | -11082.1533 | -11078.3659 |
| $E_{\mathrm{N}}$ | 9001.5341 | 9001.5840 | 9001.8675 | 9004.6837 | 9002.7529 | 8995.9116 | 8992.1390 |
| $E_{\mathrm{n}}$ | 235.6215 | 235.6290 | 235.6588 | 235.9209 | 235.7749 | 235.1954 | 234.8701 |
| 1 i |  |  |  |  |  |  |  |
| $E^{\text {T }}$ | -2 981.5947 | -2981.5953 | -2981.5982 | -2 981.6182 | -2981.6315 |  |  |
| $E_{\text {e }}$ | -15656.0401 | -15656.1216 | -15656.2985 | -15658.3358 | -15658.4500 |  |  |
| $E_{\mathrm{N}}$ | 12674.4455 | 12674.5263 | 12674.6976 | 12676.7176 | 12676.8184 |  |  |
| $E_{\text {n }}$ | 286.1286 | 286.1398 | 286.1591 | 286.3514 | 286.3859 |  |  |

${ }^{a}$ The starting geometry of each molecular conformation was taken from its crystal structure. The conformational space was sampled by varying $\theta$ in steps of $5^{\circ}$ for $0^{\circ}<\theta<90^{\circ}$. At each point a full optimization was carried out under the condition that all the ring atoms in each of two aromatic ring were kept coplanar.
energy in the FUL state of fragment P. In eq (2-2), the energy effect $\Delta E_{\sigma}^{(\pi)}$ is the response of the $\sigma$ framework to the delocalization of the $\pi$-electrons and it arises from the effects of the $\pi$-electron delocalization on the $\sigma-\pi$ space interactions expressed in terms of the Coulomb $J_{\sigma \pi}$ and exchange $K_{\sigma \pi}$ integrals. In the M-SCF scheme, the energy components $\Delta E_{p q}^{(\pi)-\lambda}$ and $\Delta E_{p}^{(\pi)-\lambda}$ are obtained from the following general expressions:

$$
\begin{array}{r}
\Delta E_{p q}^{(\pi)-\lambda}=\sum_{i, j}^{\lambda}\left(F_{i j}^{(\pi)-\lambda}+H_{i j}^{(\pi)-\lambda}\right) D_{i j}^{(\pi)-\lambda} \quad i \in \mathrm{P}, j \in \mathrm{Q} \\
E_{p}^{(\tau)-\lambda}=\sum_{i, k}^{\lambda}\left(F_{i k}^{(\pi)-\lambda}+H_{i k}^{(\pi)-\lambda}\right) D_{i k}^{(\pi)-\lambda} \quad i, k \in \mathrm{P} \\
E_{p}^{(0)-\lambda}=\sum_{i, k}^{\lambda}\left(F_{i k}^{(0)-\lambda}+H_{i k}^{(0)-\lambda}\right) D_{i k}^{(0)-\lambda} \quad i, k \in \mathrm{P} \tag{3-3}
\end{array}
$$

where $\mathbf{F}, \mathbf{H}$, and $\mathbf{D}$ are Fock, Hamiltonian, and density matrices respectively (a capital bold letter denotes, hereafter, a matrix over the complete FMO basis set); $F_{i j}^{(\pi)-\lambda}, H_{i j}^{(\pi)-\lambda}$, $D_{i j}^{(\pi)-\lambda}$ et al. are their respective elements. The various elements in eqs (3-1)-(3-2) are obtained from the RHF (restricted Hartree-Fock) computation, denoted as RHF $^{\pi}$-m in Figure 5,
for the DPI state under the following conditions: in each SCF iteration, all the elements $S_{i j}$ (the elements of the overlap integral matrix $\mathbf{S})$ and $F_{i j}(i \neq j)$ between the FMOs of the $\sigma$ type are set equal to zero except four elements, $F_{s a, s b 1}, S_{s a, s b 1}, F_{s c, s b 2}$, and $S_{s c, s b 2}$. The subscripts $s a$ and $s b 1$ in $F_{s a, s b 1}$ denote a pair of the singly occupied FMOs belonging, respectively, to two bonded fragments A and B , and the $s c$ and $s b 2(s b 1 \neq s b 2)$ a pair of those belonging to fragments C and B . The conditional RHF computation, denoted as $\mathrm{RHF}^{\pi}$-f, for the various elements in eq (3-3) was performed over the same complete FMO basis. In this computation, all the elements $S_{i j}=0.0$ and $F_{i j}=0.0(i \neq$ $j$ ) except the elements $F_{s a, s b 1}, S_{s a, s b 1}, F_{s c, s b 2}$, and $S_{s c, s b 2}$. In the conditional RHF computation, denoted as $\mathrm{RHF}^{\sigma}-\mathrm{m}$, for the various elements in the DSI state, all the $F_{i j}$ and $S_{i j}(i \neq j)$ between the FMOs of the $\pi$ type are set equal to zero. The RHF-T computation for the elements, such as $F_{i j}^{(\sigma, \pi)-\lambda}$, $H_{i j}^{(\sigma, \pi)-\lambda}$, and $D_{i j}^{(\sigma, \pi)-\lambda}$, in the FUD state was performed under the constraint, a fundamental requirement for every type of conditional RHF computation, that all the $F_{i j}$ and $S_{i j}$ between the $\pi$ and $\sigma$ FMOs are set equal to zero. All the conditions employed in each of four types of the conditional RHF computations ensure that the molecular orbitals (MOs) of the $\pi$ type are thoroughly separated from those of the $\sigma$ type.

The complete FMO basis set, in which all FMOs have correct electron occupancies, consists of CDF-MOs (closed-shell de-


Figure 3. The crystal structure of $\mathbf{1 h}$, and its rotational geometries $\mathbf{1 h} \mathbf{- R 0}, \mathbf{1 h}-\mathbf{R 4 0}, \mathbf{1 h} \mathbf{- R 9 0}, \mathbf{1 h}-\mathbf{P L}$, and $\mathbf{1 h}-\mathrm{VER}$ obtained from AM .
localized FMOs) and singly occupied OLF-MOs (opened-shell localized FMOs). The construction of this basis set is a threestep procedure: (i) three basis sets from their respective planar fragment molecules (PFM), (ii) transformation of the basis set for the PFM into that for the corresponding nonplanar fragment molecule, and (iii) the formation of a complete basis set for the optimized geometry of a molecule by the superposition of three basis sets belonging, respectively, to fragments $\mathrm{A}, \mathrm{B}$, and C .

Construction of a Complete FMO Basis Set. According to the Whangbo-Schlegel-Wolfe-Kost (WSW-K) procedure, ${ }^{20}$ i.e., a conditional UHF (unrestricted Hartree-Fock) computation for the composite system such as $\mathbf{1 h}$ followed by the Kost's localization, three groups of OLF-MOs can be characterized by the following expressions:

$$
\begin{align*}
\psi_{a i} & =\sum_{k=1}^{n a} a_{k i} \phi_{k}+\sum_{m=n a+1}^{n a+n b} a_{m i} \phi_{m}+\sum_{n=n a+n b+1}^{N} a_{n i} \phi_{n}  \tag{4-1}\\
\psi_{b j} & =\sum_{k=1}^{n a} a_{k j} \phi_{k}+\sum_{m=n a+1}^{n a+n b} a_{m j} \phi_{m}+\sum_{n=n a+n b+1}^{N} a_{n j} \phi_{n} \tag{4-2}
\end{align*}
$$

$$
\begin{equation*}
\psi_{c l}=\sum_{k=1}^{n a} a_{k l} \phi_{k}+\sum_{m=n a+1}^{n a+n b} a_{m l} \phi_{m}+\sum_{n=n a+n b+1}^{N} a_{n l} \phi_{n} \tag{4-3}
\end{equation*}
$$

where the atomic orbitals (AOs) $\phi_{k}\left(k=1,2, \ldots, n_{a}\right) \in \mathrm{A}, \phi_{m}$ $\left(m=n_{a}+1, \ldots, n_{a}+n_{b}\right) \in \mathrm{B}$, and $\phi_{n}\left(n=n_{a}+n_{b}+1, \ldots, N\right)$ $\in \mathrm{C} ; a_{k i}, a_{m i}$, and $a_{n i}$ are their coefficients. In our new procedure, the first sum term in eq (4-1), i.e., a set of the OLF-MOs $\psi_{a i}$ for the isolated fragment A , is obtained indirectly from a planar fragment molecule, denoted as FM-A in Figure 4b, using the WSW-K procedure. The FM-A resulted from the replacement of the 3-pyridyl- $\mathrm{N}=\mathrm{CH}$ - group $(\mathrm{B}+\mathrm{C})$ in $\mathbf{1 h}$ with a hydrogen atom denoted as $\mathrm{H}_{\mathrm{r}}$ while all the bond angles and bond lengths were kept unchanged with the exceptions that the value of 1.0 $\AA$ was imposed on the length of the $\mathrm{C}_{9}-\mathrm{H}_{\mathrm{r}}$ bond and the dihedral angle $\mathrm{H}_{\mathrm{r}}-\mathrm{C}_{9}-\mathrm{C}_{10}-\mathrm{C}_{11}$ was set equal to $180^{\circ}$. The 1 s AO of the $\mathrm{H}_{\mathrm{r}}$, denoted as $\psi_{\mathrm{H}}$, is an excellent singly occupied $\sigma$ FMO, and the formation of the FM-A simplifies the localization procedure greatly. However, the dihedral angles, such as the $\mathrm{C}_{8}-\mathrm{C}_{9}-\mathrm{C}_{10}-\mathrm{C}_{11}$ and $\mathrm{N}_{7}-\mathrm{C}_{1}-\mathrm{C}_{2}-\mathrm{C}_{3}$ in Figures 1 and 3, are generally less than $180^{\circ}$. Therefore, it is necessary for the OLFMOs of the $\sigma$ type to be localized once more. In the second

(a)


Fragment molecule Fragment molecule Fragment molecule FM-A FM-B FM-C

Figure 4. (a) The dissection way and the numbering system in $N$-phenylmethylene-3-pyridineamine (1h). The A-B-C dissection of 1h into a phenyl fragment (A), an imine group (B), and a 3-pyridyl fragment (C). (b) Formation of the corresponding fragment molecules denoted as FM-A, FM-B, and FM-C.
localization, all the $\pi$ OLF-MOs are kept unchanged, and the atomic overlap integral matrix s used in Kost's localization is from a nonplanar fragment molecule denoted as NFM-A. The only difference in the geometry between the FM-A and the NFM-A occurs in the angle $\mathrm{H}_{\mathrm{r}}-\mathrm{C}_{9}-\mathrm{C}_{10}-\mathrm{C}_{11}$. In the case of the NFM-A, this angle is set equal to the $\mathrm{C}_{8}-\mathrm{C}_{9}-\mathrm{C}_{10}-\mathrm{C}_{11}$ in the optimized geometry of $\mathbf{1 h}$.

However, the Kost's localization fails to ensure all the $\pi$ OLFMOs correct electronic occupancies. A conditional RHF computation, over the OLF-MOs basis set, for the NFM-A has to be performed after the Kost's localization. From this computation, a set of the CDF-MOs $\varphi_{a i}$ is obtained under the following conditions: first, all the elements $F_{i j}=0.0$ and $S_{i j}=$ $0.0\left(i \in \mathrm{~A}, j \in \mathrm{H}_{\mathrm{r}}\right)$ except two elements $F_{s a, H}$ and $S_{s a, H}$ between a pair of singly occupied OLF-MO $\psi_{s a}$ and $\psi_{H}$; second, all the intrafragment elements $F_{s a, a i}$ and $S_{s a, a i}(s a \neq a i)$ and those between the $\pi$ and $\sigma$ OLF-MOs are set equal to zero. A set of the CDF-MOs and a singly occupied OLF-MO $\psi_{s a}$ form a FMO basis set $\Phi_{a i}$ for fragment A. All $\Phi_{a i}$ have now correct electronic occupancies, and the $\pi$ type of $\Phi_{a i}$ has been thoroughly separated from the $\sigma$ type. A FMO basis set $\Phi_{b j}$ for fragment B and that $\Phi_{c l}$ for fragment C are obtained in a similar way. In the case of fragment B, there are two singly occupied OLF-MOs $\psi_{s b 1}$ and $\psi_{s b 2}$. A singly occupied OLFMO for fragment C is denoted as $\psi_{s c}$. At last, according to the characteristics as shown in eqs (4-1)-(4-3), a complete FMO basis set is formed by the superposition of three basis sets, $\Phi_{a i}$, $\Phi_{b j}$, and $\Phi_{c l}$. In the meantime, all the coefficients corresponding to those $a_{m i}, a_{n i}, a_{k j}, a_{n j}, a_{k l}$, and $a_{m l}$ in eqs (4-1)-(4-3) are set equal to zero.

In the case of larger molecules such as $\mathbf{1 a} \mathbf{- 1} \mathbf{j}$, the calculations involving larger basis sets such as $6-31 \mathrm{G}$ et al. are extremely costly. In this work, the complete FMO basis set and the various orbital interaction energies were constructed and calculated using the ab initio SCF-MO computation program at the STO-3G level. The various rotational geometries were optimized using AM1. It should be stressed that during the period of any ab initio SCF iteration, the geometries of a molecule, its fragments and fragment molecules were no longer optimized.

## Results and Discussion

Geometry Optimization. In our practical calculations, the rotational geometries of each of STB-type 1 were optimized using the various semiempirical calculations such as AM1, MNDO, MINDO/3, and PM3. ${ }^{12}$ Our practical calculations and recent literature show that the AM1 method appears to be most suitable. ${ }^{3,21}$ However, AM1 cannot treat correctly all the molecules. In fact, the abnormal difference in the twist angle $\phi$ between the experiment and AM1 calculation occurs in molecule 1f. According to the energy data in Table 2, it may result from its rather flat potential energy.

The starting geometry of each molecular conformation was taken from the crystal structure, and the geometry optimizations for the various rotational conformers were experimentally carried out under the following two models: (i) the full optimization (Model I); (ii) all the dihedral angles are kept to be $0^{\circ}$ or $180^{\circ}$ (Model II). In addition, the H and ring atoms in each of two aromatic rings were kept on same plane, and the twist angle $\theta$ in a given rotational conformer was kept unchanged in above two models. Our practical calculations show that of all the dihedral angles, only the angle $\mathrm{P}-\mathrm{C}_{1}-\mathrm{X}-\mathrm{Z}$ has the greatest effect on the preferential geometry, and a larger angle $\theta$ corresponds generally to a larger deviation of the angle $\mathrm{N}_{7}-$ $\mathrm{C}_{1}-\mathrm{X}-\mathrm{Z}(\mathrm{X}, \mathrm{Z}=\mathrm{C}, \mathrm{N})$ from $180^{\circ}$ (see Figures $1-3$ ). Therefore, the whole aromatic ring with a substituent group such as $-\mathrm{NO}_{2},-\mathrm{NH}_{2}$, or -Cl can be considered approximately as a planar fragment, which will greatly simplify our computational procedure.

When $\alpha \neq 0$ and $\theta \neq 0$, there should be eight types of the FMO interactions. However, the $\sigma-\pi$ interaction results in the mixture of the $\sigma$ and $\pi$ FMOs and will not be considered here.
$\pi$-System Is Most Destabilized in the DPI State of Coplanar Geometry. According to the definitions of the Coulomb and exchange integral matrices $\mathbf{J}$ and $\mathbf{K}$, we have the following theoretical expressions for the elements in eqs (31) $-(3-3) .{ }^{22}$

$$
\begin{align*}
& F_{i j}^{(\pi)-\lambda}=H_{i j}^{(\pi)-\lambda}+\sum_{m} \sum_{n} D_{m n}^{(\pi)-\lambda}[(i j, m n)-1 / 2(i m, j n)]  \tag{5-1}\\
& F_{i k}^{(\pi)-\lambda}=H_{i k}^{(\pi)-\lambda}+\sum_{m} \sum_{n} D_{m n}^{(\pi)-\lambda}[(i k, m n)-1 / 2(i m, k n)]  \tag{5-2}\\
& F_{i k}^{(0)-\lambda}=H_{i k}^{(0)-\lambda}+\sum_{m} \sum_{n} D_{m n}^{(0)-\lambda}[(i k, m n)-1 / 2(i m, k n)] \tag{5-3}
\end{align*}
$$

The constrained conditions in the $\mathrm{RHF}^{\pi}$-f and $\mathrm{RHF}^{\pi}$-m ensure all the $D_{m n}^{(\pi)-\sigma}$ and $D_{m n}^{(0)-\sigma}(m \neq n)$ are equal to zero except those between two pairs of the single occupied FMOs. In these cases, the effect of the $\sigma$-electron delocalization on the $\pi$ system has been eliminated as far as possible.

In order to get deeper insight into the conjugation effect on the original energies $E_{p}^{(0)-\pi}$, the energy effect $\Delta E_{\pi}^{(\pi)}(\theta)$ including its components $\Delta E_{p q}^{(\pi)-\pi}(\theta)$ and $\Delta E_{p}^{(\pi)-\pi}(\theta)$ were calculated (Tables 3 and 4). In accord with the classic viewpoint, the conjugation energy $\Delta E_{a b+b c}^{(\pi)-\pi}(\theta)$ is most stabilizing at the coplanar geometry, and weakens with the rotation of fragment C about the $\mathrm{C}_{1}-\mathrm{N}_{7}$ bond. The absolute value ( $|-1.1369|$ hartree $)$ of $\Delta E_{a b+b c}^{(\pi)-\pi}$ in the coplanar geometry is greatest of all the rotational geometries listed in Table 3, and its minimum value, about $|-0.00099|$ hartree, occurs in the vertical geometry with $\alpha=\theta=90^{\circ}$. However, as shown by the data in Tables 3 and 4, the conjugation reduces, without exception, the original $\pi$ energy $E_{p}^{(\mathbf{o})-\pi}$ of each of fragments, and, moreover, the energy


Figure 5. The thermodynamic cycle for the orbital interactions and the definitions of the various energy differences. The numbers in parentheses are the values (hartrees) of the total electronic energies in four hypothetical states (FUL, DPI, DSI, and FUD) of the copolanar geometry of $\mathbf{1 h}$.

TABLE 3: Energy Gain $\Delta E_{p q}^{(\tau)-\pi}$, Energy Losses $\Delta E_{p}^{(\pi)-\pi}$, Total $\pi$ and $\sigma$ Interaction Energies $\Delta E_{\pi}^{(\pi)}$ and $\Delta E_{\sigma}^{(\tau)}$, and Total Electronic Energies $E_{\boldsymbol{\pi}}^{(\pi)}$ and $E_{\sigma}^{(\pi)}$ in the DPI State of 1 h , and Their Changes with the Rotation of Fragment $\mathbf{C}$ (Energy in Hartrees)

| angle (deg) |  | $\Delta E_{a b}^{(\pi)-\pi}$ | $\Delta E_{b c}^{(\pi)-\pi}$ | $\Delta E_{a}^{(\pi)-\pi}$ | $\Delta E_{b}^{(\pi)-\pi}$ | $\Delta E_{c}^{(\pi)-\pi}$ | $\Delta E_{\pi}^{(\pi)}$ | $\Delta E_{\sigma}^{(\pi)}$ | $E_{\pi}^{(\pi)}$ | $E_{\sigma}^{(\pi)}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\theta$ | $\alpha$ |  |  |  |  |  |  |  |  |  |
| Model II of Optimizing |  |  |  |  |  |  |  |  |  |  |
| 0 | 0 | -0.544 29 | -0.592 56 | 0.55015 | 0.43380 | 0.24219 | 0.08867 | -0.076 47 | -134.7154 | -1167.2741 |
| 10 | 0 | $-0.54214$ | -0.574 64 | 0.54937 | 0.42035 | 0.23403 | 0.08663 | -0.074 58 | -134.7285 | -1167.3118 |
| 30 | 0 | $-0.52831$ | $-0.44513$ | 0.54442 | 0.32117 | 0.17943 | 0.07133 | -0.060 44 | -134.8300 | -1167.6070 |
| 50 | 0 | -0.504 27 | -0.248 88 | 0.53271 | 0.15833 | 0.10783 | 0.04558 | -0.036 63 | -134.9147 | -1167.6222 |
| 90 | 0 | -0.474 11 | $-0.00068$ | 0.51663 | -0.054 51 | 0.02301 | 0.01034 | -0.003 35 | -134.9125 | -1167.0489 |
| 90 | 90 | $-0.00030$ | -0.000 69 | 0.00034 | 0.00049 | 0.00020 | 0.00005 | -0.000 08 | -135.0351 | -1167.1675 |
| Model I of Optimizing |  |  |  |  |  |  |  |  |  |  |
| 0 |  | -0.541 44 | -0.592 20 | 0.54748 | 0.43271 | 0.24236 | 0.08854 | -0.076 36 | -134.7147 | -1167.2647 |
| 10 |  | $-0.53662$ | $-0.57443$ | 0.54406 | 0.41805 | 0.23570 | 0.08640 | -0.074 40 | -134.7296 | -1167.3036 |
| 30 |  | $-0.52665$ | -0.454 66 | 0.54247 | 0.32235 | 0.18871 | 0.07189 | -0.061 03 | -134.8072 | -1167.4844 |
| 50 |  | $-0.50565$ | -0.27193 | 0.53261 | 0.17214 | 0.12131 | 0.04831 | -0.039 10 | -134.8507 | -1167.3113 |
| 90 |  | -0.473 32 | -0.002 91 | 0.51633 | -0.056 07 | 0.02567 | 0.00968 | -0.002 73 | -134.8104 | -1166.4864 |

gain $\Delta E_{a b+b c+c a}^{(\pi)-\pi}(\theta)$ is insufficient to compensate for the total energy loss $\Delta E_{a+b+c}^{(\pi)-\pi}(\theta)$. The total $\pi$ energy effect $\Delta E_{\pi}^{(\pi)}(\theta)$ is destabilizing. The $\Delta E_{\pi}^{(\pi)}\left(0^{\circ}\right)$ of $\mathbf{1 h}$ is large up to $55.64 \mathrm{kcal} /$ mol. At the vertical geometry, there should be no $\pi$ interactions between fragments except the long distance interaction between fragments A and C. The calculation results are $\Delta E_{a b+b c}^{(\pi)-\pi}=$ $-0.62 \mathrm{kcal} / \mathrm{mol}$ and $\Delta E_{\pi}^{(\pi)}=0.031 \mathrm{kcal} / \mathrm{mol}$ (Table 3).

As shown by the data of $\Delta E_{\sigma}^{(\pi)}(\theta)$ in Tables 3 and 4, the $\sigma$ framework is stabilized owing to the $\sigma-\pi$ space interactions, while the $\pi$ system itself is destabilized due to the $\pi$-electron interactions between fragments. However, this energy gain $\Delta E_{\sigma}^{(\pi)}(\theta)$ is still insufficient to compensate for the $\pi$ energy $\operatorname{loss} \Delta E_{\pi}^{(\pi)}(\theta)$. The total energy effect $\Delta E_{\pi}^{(\pi)}(\theta)+\Delta E_{\sigma}^{(\pi)}(\theta)$ is destabilizing. At the coplanar geometry of $\mathbf{1 h}$, for example, its value ( $7.66 \mathrm{kcal} / \mathrm{mol}$ ) is greatest, and the total electronic energy ( -1301.9895 hartrees) in the DPI state is the highest of four hypothetical electronic states (see Figure 5). It might be a reason why the symmetrization of the phenyl ring in 1h-VER is better than that of $\mathbf{1 h} \mathbf{- R 0}$ (Figure 3).

Destabilization of the $\pi$-System in the DPI State Is Due to $\pi$-Electron Delocalization. Electron delocalization is an important concept in modern organic chemistry. One problem is that "delocalization" is not directly measurable and there is no single definition underlying the use of this concept throughout chemistry. ${ }^{23}$ As shown by Figure 6, the charge transfer (CT)
mixes the occupied FMO of one fragment with the vacant FMO of the other and vice versa, and one of two exchange (EX) energies is associated with the interaction between the occupied FMOs. According to the Morokuma definitions, ${ }^{15}$ these two interactions cause $\pi$-electron delocalization between fragments. Based on the PMO expression for two-electron interaction energy, ${ }^{24}$ the CT energy $\Sigma_{o v}^{p q}$ (Figure 6) can be defined as the energy gain of fragment $P$, and it is associated with the interaction which causes the delocalization of the $\pi$-electrons from P to Q . Comparison of the values of the $\Sigma_{p}^{2}$ and the net $\pi$-electron charge $D_{\rho}^{(\pi)}$ (Table 5) and inspection of their signs indicate that the quantity $\Sigma_{p}^{2}$, as defined by eqs (6-1)-(6-3), can be used to measure, indirectly, the net charge transfer.

$$
\begin{gather*}
\Sigma_{a}^{2}=\Sigma_{o v}^{b a}-\Sigma_{o v}^{a b}  \tag{6-1}\\
\Sigma_{c}^{2}=\Sigma_{o v}^{b c}-\Sigma_{o v}^{c b}  \tag{6-3}\\
\Sigma_{b}^{2}=-\left(\Sigma_{a}^{2}+\Sigma_{c}^{2}\right) \tag{6-2}
\end{gather*}
$$

whether fragment P is a +M or -M group depends upon the sign of $\Sigma_{p}^{2}$. The signs of the $D_{a}^{(\pi)}$ and $\Sigma_{a}^{2}$ both are positive without exception; fragment A is +M group as far as twoelectron interaction is concerned. On the other hand, it is difficult to determine the contributions made by each of two

TABLE 4: Energy Gain $\Delta E_{a b+b c}^{(\pi)-\pi}$, Energy Losses $\Delta E_{p}^{(\pi)-\pi}$, CT Energy $\Sigma_{o v}^{c b}$, Total $\pi$ and $\sigma$ Interaction Energies $\Delta E_{\pi}^{(\pi)}$ and $\Delta E_{\sigma}^{(\pi)}$, Total Electronic Energies $E_{\pi}^{(\pi)}$ and $E_{\sigma}^{(\tau)}$ in the DPI State of Stilbene-like Species, and the Changes with the Rotation of Fragment C (Energy in Hartrees)

| ang | eg) |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\theta$ | $\alpha$ | $\Delta E_{a b+b c}^{(\pi)-\pi}$ | $\Delta E_{a}^{(\pi)-\pi}$ | $\Delta E_{b}^{(\pi)-\pi}$ | $\Delta E_{c}^{(\pi)-\pi}$ | $\Sigma_{o v}^{c b_{\mathrm{a}}}$ | $\Delta E_{\pi}^{(\pi)}$ | $\Delta E_{\sigma}^{(\pi)}$ | $E_{\pi}^{(\pi)}$ | $E_{\sigma}^{(\pi)}$ | model |
| Compound 1a |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 0 | -1.15654 | 0.39298 | 0.46376 | 0.39181 | -0.469 82 | 0.09147 | -0.077 24 | -132.1603 | -1131.6589 | II |
| 5 | 5 | -1.14670 | 0.39012 | 0.45876 | 0.38918 | -0.466 52 | 0.09083 | -0.076 71 | -132.1687 | -1131.6866 | I |
| 20 | 20 | -1.010 44 | 0.35121 | 0.39041 | 0.35051 | -0.419 28 | 0.08169 | -0.068 87 | -132.2658 | -1131.9565 | I |
| Compound 1j |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 0 | $-1.08610$ | 0.37063 | 0.44310 | 0.35974 | -0.424 78 | 0.08706 | -0.074 61 | -134.5834 | -1166.7678 | II |
| 5 |  | -1.08124 | 0.37070 | 0.44027 | 0.35719 | -0.42171 | 0.08661 | -0.074 22 | -134.5856 | -1166.7696 | I |
| 20 |  | $-1.01504$ | 0.37317 | 0.40328 | 0.31936 | $-0.37672$ | 0.08048 | $-0.06861$ | -134.6308 | -1166.9018 | I |
| Compound 1h |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 0 | $-1.13685$ | 0.55015 | 0.43380 | 0.24219 | $-0.40170$ | 0.08868 | $-0.07662$ | -134.7154 | -1167.2741 | II |
| 5 |  | -1.129 79 | 0.54820 | 0.42952 | 0.24048 | -0.398 80 | 0.08806 | -0.075 98 | -134.7182 | -1167.2761 | I |
| Compound if |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 0 | $-1.18751$ | 0.43623 | 0.60473 | 0.23278 | $-0.39947$ | 0.08597 | -0.075 19 | -193.9805 | -1588.3054 | II |
| 5 |  | -1.182 36 | 0.43596 | 0.60138 | 0.23087 | -0.396 55 | 0.08561 | -0.074 82 | -193.9824 | -1588.3087 | I |
| 20 |  | $-1.11567$ | 0.43565 | 0.55478 | 0.20594 | -0.356 36 | 0.08050 | -0.069 99 | -194.0056 | -1588.3379 | I |
| Compound 1e |  |  |  |  |  |  |  |  |  |  |  |
| 5 |  | $-1.17111$ | 0.53428 | 0.54425 | 0.17957 | -0.378 47 | 0.08674 | -0.075 76 | -168.3997 | -1754.1976 | I |
| 20 |  | $-1.10493$ | 0.53053 | 0.49518 | 0.16074 | -0.340 69 | 0.08128 | $-0.07068$ | -168.4250 | -1754.2161 | I |
| Compound $1 \mathrm{~g}^{\text {b }}$ |  |  |  |  |  |  |  |  |  |  |  |
| ${ }_{5}$ | 0 | -1.236 37 | 0.82343 | 0.43183 | 0.05622 | $-0.34569$ | 0.07471 | -0.064 45 | -158.8848 | -1292.3778 | II |
| 5 |  | -1.23194 | 0.82273 | 0.42797 | 0.05595 | -0.343 45 | 0.07431 | -0.064 10 | -158.8863 | -1292.3785 | I |
| 20 |  | $-1.16373$ | 0.81281 | 0.36994 | 0.04961 | -0.308 33 | 0.06828 | $-0.05835$ | -158.9106 | -1292.4070 | I |
| Compound 1i |  |  |  |  |  |  |  |  |  |  |  |
| 5 |  | $-1.17004$ | 0.49291 | 0.71134 | 0.04827 | -0.330 88 | 0.08229 | -0.072 37 | -195.1545 | -1605.7823 | I |
| 20 |  | $-1.10563$ | 0.48824 | 0.64997 | 0.04436 | -0.29789 | 0.07676 | -0.067 37 | -195.1867 | -1605.8563 | I |

${ }^{a}$ The energy effect $\Sigma_{o v}^{c b}$ will be defined and used in the next section. ${ }^{b}-\mathrm{N}(\mathrm{Me})_{2}$ group in $\mathbf{1 g}$ has been replaced with a planar $-\mathrm{NH}_{2}$.


| P, Occ | P, Occ P, Vac Q, Occ Q, Vac |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\sum_{o o}^{p p}$ ESX | $\begin{aligned} & \sum_{o v}^{p p} \\ & \operatorname{PLX} \end{aligned}$ | $\sum_{\mathrm{EX}}^{p q}$ | $\underset{o v}{\sum_{o v}^{p q}}$ |
| P, Vac | $\sum_{\text {PLX }}^{p p}$ | $\sum_{\text {ESX }}^{p p}$ | $\sum_{\text {cT }}^{p q}$ | $\sum_{\text {EX }}^{\sum_{w v}^{p q}}$ |
| Q, Occ | $\sum_{\text {EX }}^{\text {co }}$ |  | $\sum_{\text {ESX }}^{\text {aq }}$ | $\sum_{\text {PLX }}^{\underline{O V}}$ |
| Q, Vac | $\sum_{\text {CT }}^{\text {co }}$ (p |  | $\sum_{\text {PLX }}^{\text {Pq }}$ | $\sum_{\text {ESX }}^{M q}$ |

Figure 6. Morokuma's definitions of the FMO interactions between fragments P and $\mathrm{Q}(\mathrm{P}, \mathrm{Q}=\mathrm{A}, \mathrm{B}, \mathrm{C})$.
fragments to the EX energy $\Sigma_{o o}^{p q}$. Referring to the method for calculating the gross AO's charge, ${ }^{25}$ the EX energy might be able to be divided evenly into two parts $\Sigma_{o o}^{p q}=(1 / 2) \Sigma_{o o}^{p q}+$ $(1 / 2) \sum_{o o}^{q p}$ (Table 5); still we cannot say which fragment is a -M group as far as the four-electron interaction is concerned.

A comparison of the data in Table 5 with the corresponding $\Delta E_{p}^{(\pi)-\pi}(\theta)$ in Table 3 shows that the energy losses $\Delta E_{b}^{(\pi)-\pi}(\theta)$ and $\Delta E_{c}^{(\pi)-\pi}(\theta)$ become larger while the absolute values of the $\Sigma_{o v}^{b c}(\theta)+\Sigma_{o v}^{b a}(\theta)$ and the $\Sigma_{o v}^{c b}(\theta)$ increase with the geometry of $\mathbf{1 h}$ getting flatter. At the coplanar geometry, for example, the $\Sigma_{o v}^{b c}\left(0^{\circ}\right)+\Sigma_{o v}^{b a}\left(0^{\circ}\right)(-0.87472$ hartree $)$ and $\Sigma_{o v}^{c b}\left(0^{\circ}\right)(-0.40187)$ are most stabilizing, and the corresponding $\Delta E_{b}^{(\pi)-\pi}\left(0^{\circ}\right)(0.24236)$ and $\Delta E_{c}^{(\pi)-\pi}\left(0^{\circ}\right)(0.43271)$ both are most destabilizing. In Table 4, there are seven sets of the data listed in increasing order of the value of $\Sigma_{o v}^{c b}\left(0^{\circ}\right)$ in each of seven compounds. Table 4 shows further that from compound 1a to $\mathbf{1 i}$, the value of the $\Delta E_{c}^{(\pi)-\pi}\left(0^{\circ}\right)$ decreases as the absolute value of the $\Sigma_{o v}^{c b}\left(0^{\circ}\right)$ decreases. In molecule 1a, for example, the absolute value $(|-0.4698|$ hartree $)$ of the $\Sigma_{o v}^{c b}\left(0^{\circ}\right)$ and the value ( 0.3918 hartree) of the corresponding $\Delta E_{c}^{(\pi)-\pi}\left(0^{\circ}\right)$ both are greatest, and the smallest values $(|-0.3332|$ and 0.0484 hartree) of these two energies both occur in $\mathbf{1 i}$. This comparison also indicates that in a given geometry with the $\theta \neq 50^{\circ}$, a larger energy loss $\Delta E_{p}^{(\pi)-\pi}(\theta)$ corresponds to a larger value of the $\Sigma_{p}^{2}(\theta)$. In the $\theta=0^{\circ}$ geometry (Model I) of $\mathbf{1 h}$, for example, the value of the $\Sigma_{p}^{2}\left(0^{\circ}\right)$ decreases in the sequence: $\Sigma_{a}^{2}\left(0^{\circ}\right)=0.13570$ hartree $>\Sigma_{b}^{2}\left(0^{\circ}\right)=-0.01746>\Sigma_{c}^{2}\left(0^{\circ}\right)=$ -0.11824 , and the value of the corresponding $\Delta E_{p}^{(\pi)-\pi}\left(0^{\circ}\right)$ decreases in the same sequence: $\Delta E_{a}^{(\pi)-\pi}\left(0^{\circ}\right)=0.54748$ hartree $>\Delta E_{b}^{(\pi)-\pi}\left(0^{\circ}\right)=0.43271>\Delta E_{c}^{(\pi)-\pi}\left(0^{\circ}\right)=0.24236$.

Every $\pi$ system with $\Sigma_{p q}^{o v}(\theta)<0.0$ is destabilized (except $\Delta E_{b}^{(\pi)-\pi}\left(90^{\circ}\right)$ ), and which one is most destabilized depends upon their values of $\Sigma_{p}^{2}(\theta)$.

TABLE 5: CT Energies $\Sigma_{o v}^{p q}$, Net CT Energies $\Sigma_{P}^{2}$, EX Energies $\Sigma_{o o}^{p q}$ Occurring in Five Typical Geometries (Model I) of 1h, and the Net $\boldsymbol{\pi}$-Electron Charge $D_{p}^{(\pi)}$ on Each of Three Fragments (Energy in Hartrees)

|  | $\theta=0^{\circ}$ | $\theta=10^{\circ}$ | $\theta=30^{\circ}$ | $\theta=50^{\circ}$ | $\theta=90^{\circ}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Fragment A |  |  |  |  |  |
| $\Sigma_{\text {ov }}^{a b}$ | -0.490 32 | -0.488 31 | -0.495 35 | $-0.50018$ | $-0.50393$ |
| $\Sigma_{a}^{2}$ | 0.13570 | 0.13646 | 0.14720 | 0.16095 | 0.18064 |
| $0.5 \Sigma_{o o}^{a b}$ | 0.16241 | 0.16210 | 0.16666 | 0.17187 | 0.17742 |
| $D_{a}^{(\pi)}$ | 0.02622 | 0.02614 | 0.02660 | 0.02681 | 0.02703 |
| Fragment B |  |  |  |  |  |
| $\Sigma_{o v}^{b a}+\Sigma_{o v}^{b c}$ | $-0.87472$ | -0.856 96 | -0.749 94 | $-0.58052$ | -0.325 57 |
| $\Sigma_{b}^{2}$ | $-0.01746$ | $-0.02143$ | -0.052 91 | $-0.10312$ | -0.180 62 |
| $0.5\left(\Sigma_{o o}^{b a}+\Sigma_{o o}^{b c}\right)$ | 0.35036 | 0.34503 | 0.31319 | 0.26089 | 0.17805 |
| $D_{b}^{(\pi)}$ | -0.013 49 | -0.013 78 | -0.016 43 | -0.020 58 | $-0.02712$ |
| Fragment C |  |  |  |  |  |
| $\Sigma_{o v}^{c b}$ | -0.401 87 | $-0.39008$ | $-0.30750$ | -0.183 46 | -0.002 27 |
| $\Sigma_{c}^{2}$ | -0.118 24 | $-0.11503$ | -0.094 29 | $-0.05784$ | 0.00060 |
| $0.5 \Sigma_{\text {oo }}$ | 0.18795 | 0.18293 | 0.14653 | 0.08902 | 0.00063 |
| $D_{c}^{(\pi)}$ | $-0.01273$ | -0.012 36 | -0.010 17 | -0.006 23 | 0.00009 |

TABLE 6: QMRE of 1 h , Its $\pi$ and $\sigma$ Components $\Delta E_{\pi}^{\mathrm{Q}}$ and $\Delta E_{\sigma}^{\mathrm{Q}}$, Total $\boldsymbol{\pi}$ and $\sigma$ Electronic Energies $E_{\pi}^{(\pi, \sigma)}$ and $E_{\sigma}^{(\pi, \sigma)}$ in the FUD State, and Their Changes with the Rotation of Fragment C (Energy in Hartrees)

| angle (deg) |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\theta$ | $\alpha$ | QMRE | $\Delta E_{\pi}^{\mathrm{Q}}$ | $\Delta E_{\sigma}^{\mathrm{Q}}$ | $E_{\pi}^{(\pi, \sigma)}$ | $E_{\sigma}^{(\pi, \sigma)}$ |
| 0 | 0 | 0.00844 | -0.08313 | 0.09157 | -134.66180 | -1167.96579 |
| 350 | 0 | 0.00823 | -0.08498 | 0.09321 | -134.67440 | -1168.00613 |
| 330 | 0 | 0.00694 | -0.09935 | 0.10629 | -134.77234 | -1168.31901 |
| 310 | 0 | 0.00489 | -0.12524 | 0.13013 | $-134.8545^{a}$ | $-1168.35751^{a}$ |
| 270 | 0 | 0.00287 | -0.16132 | 0.16419 | -134.85151 | -1167.80582 |

${ }^{a}$ Maximal absolute values.

TABLE 7: QMRE of Stilbene-like Species, and Their $\pi$ and $\sigma$ Components $\Delta E_{\pi}^{Q}$ and $\Delta E_{\sigma}^{Q}$ at the Planar Geometry (Hartrees)

| compds | QMRE | $\Delta E_{\pi}^{\mathrm{Q}}$ | $\Delta E_{\sigma}^{\mathrm{Q}}$ |
| :---: | :---: | ---: | :---: |
| $\mathbf{1 a}$ | 0.01410 | 0.00927 | 0.00483 |
| $\mathbf{1 j}$ | 0.00941 | -0.06570 | 0.07511 |
| $\mathbf{1 h}$ | 0.00844 | -0.08313 | 0.09157 |
| $\mathbf{1 e}$ | 0.00777 | -0.04956 | 0.05737 |
| $\mathbf{1}$ | 0.00770 | -0.05559 | 0.06329 |
| $\mathbf{1 i}$ | 0.00684 | -0.04125 | 0.04809 |
| $\mathbf{1 g}$ | 0.00630 | -0.08324 | 0.08954 |

The Quantum Mechanical Resonance Energy (QMRE) of Stilbene-like Species Is Destabilizing. According to the original definition, ${ }^{26}$ the QMRE of a delocalized system in a given geometry of benzene is the difference between the energy of the true ground state and the energy of a single Kekule structure. In this work, it is defined as the difference in the electronic energy between the FUD and DSI states. As shown by Tables 6 and 7, the QMRE of each of STB-type $\mathbf{1}$ is destabilizing. The QMRE ( 0.00844 hartree) of $\mathbf{1 h}$, for example, is most destabilizing at its planar geometry (Table 6), and its value monotonically decreases with the rotation of fragment $C$. A comparison of the data in Table 7 with those in Table 4 and Table 1 shows that of all molecules listed in the tables, a larger QMRE ( $>0.008$ hartree), such as those $0.0141,0.0094$, and 0.0084 hartree, respectively, in $\mathbf{1 a}, \mathbf{1} \mathbf{j}$, and $\mathbf{1 h}$ (Table 7) corresponds generally to a larger $\Sigma_{o v}^{c b}\left(0^{\circ}\right)$ and to a larger sum $\left(\phi+\alpha>35^{\circ}\right)($ Table 1).
It is known that benzene is strongly stabilized by the QMRE. ${ }^{27}$ In order to make a comparison between the QMREs of benzene and molecules of type $\mathbf{1}$, and to understand the role of the QMRE with regard to molecular geometry and chemical reactivity, the distortion of the benzene geometry, denoted as $d_{S H}$, is considered in this work, and the various energies
occurring in six typical $d_{S H}$ geometries were calculated (Table 8). The $d_{S H}$ distortion was previously investigated by Shaik and Hiberty. ${ }^{28}$ The geometries $d_{S H} \neq 0.0 \AA$ arise from variations in alternating CC bond lengths within the constraint that the contribution of the nuclear repulsion to the total energy remains constant, equal to that of the $d_{S H}=0.0 \AA$ geometry. The $d_{S H}$ $=0.1644 \AA$ geometry resembles an idealized cyclohexatriene structure of alternating single and double CC bond lengths $R_{c c}^{\prime}$ and $R_{c c}$ (see Table 8). In our PMO calculation, a distorted benzene molecule was dissected into three ethylenic fragments A, B, and C. In each of three fragments, the length of the CC double bond was equal to that of the shorter $R_{c c}$ in the composite system. Table 8 shows that the QMRE is most stabilizing at the $d_{S H}=0.0 \AA$ geometry and monotonically weakens as the carbon framework is increasingly distorted away from the $d_{S H}$ $=0.0 \AA$. At the $d_{S H}=0.0 \AA$ geometry, for example, the QMRE is $-43.28 \mathrm{kcal} / \mathrm{mol}$, and it is the average of the spectroscopy value ${ }^{29 \mathrm{a}}(-50 \mathrm{kcal} / \mathrm{mol})$ and that $(-36 \mathrm{kcal} / \mathrm{mol})^{29 \mathrm{~b}}$ suggested by thermochemical measures. However, the detail energy partition shows that the QMRE is a sum of two components $\Delta E_{\sigma}^{\mathrm{Q}}=E_{\sigma}^{(\tau, \sigma)}-E_{\sigma}^{(\sigma)}$ and $\Delta E_{\pi}^{\mathrm{Q}}=E_{\pi}^{(\pi, \sigma)}-E_{\pi}^{(\sigma)}$. Whether the QMRE is stabilizing or destabilizing depends upon the response, expressed in terms of the $\Delta E_{\sigma}^{\mathrm{Q}}\left(d_{S H}\right)$ and $\Delta E_{\sigma}^{\mathrm{Q}}(\theta)$, respectively, of the $\sigma$ frameworks to the delocalization of the $\pi$-electrons. In the case of STB-type $\mathbf{1}, \Delta E_{\sigma}^{\mathrm{Q}}(\theta)$ is always destabilizing and its value is slightly larger than the absolute value of the corresponding $\Delta E_{\pi}^{\mathrm{Q}}(\theta)$ which is generally stabilizing except for that in 1a. Conversely, the $\Delta E_{\sigma}^{\mathrm{Q}}\left(d_{S H}\right)$, as shown by the data in Table 8 , is always stabilizing, and the $\Delta E_{\pi}^{\mathrm{Q}}\left(d_{S H}\right)$ is generally destabilizing except that in the $d_{S H}=0.0 \AA$ geometry of benzene. Particularly, the absolute value ( $|-0.0533|$ hartree $)$ of the $\Delta E_{\sigma}^{\mathrm{Q}}\left(d_{S H}=0.0\right)$ is about three time larger than that ( $|-0.0177|$ hartree $)$ of the $\Delta E_{\pi}^{\mathrm{Q}}(0.0)$. Therefore, it is the $\sigma$

TABLE 8: QMRE (kcal/mol) of Benzene, Its Components $\Delta E_{\pi}^{Q}$ and $\Delta E_{\sigma}^{Q}$, Electronic Energies $E_{\pi}^{(\sigma)}$ and $E_{\sigma}^{(\sigma)}$ in the DSI State, Those $E_{\pi}^{(\pi, \sigma)}$ and $E_{\sigma}^{(\tau, \sigma)}$ in the FUD State, and Their Changes along the $\boldsymbol{d}_{S H}$ Distortion (Energy in Hartrees except for QMRE)

| $d_{S H}(\AA)$ | 0.0 | 0.0403 | 0.0811 | 0.1224 | 0.1644 | 0.2070 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $R_{c c}$ (short) | 1.40 A | 1.38 | 1.36 | 1.34 | 1.32 | 1.30 |
| $R_{c c}$ (long) | 1.40 Å | 1.4203 | 1.4411 | 1.4624 | 1.4844 | 1.5070 |
| QMRE | -43.281875 | -31.083 080 | -20.865 963 | -12.554 593 | -5.868 474 | -0.626 882 |
| $\Delta E_{\pi}^{\mathrm{Q}}$ | -0.017 645 | 0.001388 | 0.015810 | 0.026050 | 0.032805 | 0.036767 |
| $\Delta E_{\sigma}^{\text {Q }}$ | -0.051 329 | -0.050 922 | -0.049 062 | -0.046 057 | -0.042 157 | -0.037 766 |
| $E_{\pi}^{(\sigma)}$ | -39.744 438 | -39.765 388 | -39.786 453 | -39.807 735 | -39.827 721 | -39.847 374 |
| $E_{\sigma}^{(\sigma)}$ | -391.040 527 | -391.036 011 | -391.029 022 | -391.020 599 | -391.001 709 | -390.978 485 |
| $E_{\pi}^{(\pi, \sigma)}$ | -39.762 085 | -39.764 000 | -39.770 645 | -39.781 689 | -39.794 918 | -39.810 608 |
| $E_{\sigma}^{(\pi, \sigma)}$ | -391.091858 | -391.086 914 | -391.078 094 | -391.066 681 | -391.043884 | -391.016 266 |

TABLE 9: Occupied $\boldsymbol{\pi}$ MOs and Energy Changes along the $\boldsymbol{d}_{S H}$ Distortion (Energy in Hartrees) ${ }^{a}$

| $d_{S H}(\AA)$ | 0.0 | 0.0403 | 0.0811 | 0.1224 | 0.1644 | 0.2070 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 21st (HOMO) | -0.33163 | -0.33556 | DSI State <br> -0.33977 <br>  <br> 21st (HOMO) | -0.27824 | -0.27902 | FUD State |
| 17th | -0.28137 | -0.34428 | -0.34904 | -0.35410 |  |  |
|  | -0.45321 | -0.45321 | -0.45327 | -0.28513 | -0.29010 | -0.29609 |
| 1th | -0.45 | -0.45375 | -0.45429 |  |  |  |

${ }^{a}$ In the DSI state, three occupied $\pi$ MOs, 21st, 20th, and 19th, are degenerate. There are doubly degenerate levels, 21 st and 20th, in the FUD state.

TABLE 10: Total Electronic Energy $E_{\mathrm{e}}$, Nuclear Repulsion $E_{v}$, Total Molecular Energy $\boldsymbol{E}^{\mathrm{T}}$, Potential Energies $\boldsymbol{R} E_{\pi}^{(\pi)}$ and $\boldsymbol{R} E_{\sigma}^{(\boldsymbol{\sigma})}$, and Electronic Energies $\boldsymbol{E}_{\boldsymbol{\pi}}^{(\boldsymbol{\sigma})}$ and $\boldsymbol{E}_{\boldsymbol{\sigma}}^{(\boldsymbol{\sigma})}$ in the DSI State of Five Typical Geometries of $\mathbf{1 h}$ (Energy in Hartrees)

| $\theta$ (deg) | $R E_{\pi}^{(\pi)}$ | $R E_{\sigma}^{(\sigma)}$ | $E_{\pi}^{(\sigma)}$ | $E_{\sigma}^{(\sigma)}$ | $E_{\text {e }}$ | $R E_{\text {e }}$ | $E_{v}$ | $E^{\text {T }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model I of Optimizing |  |  |  |  |  |  |  |  |
| $0^{a}$ | 0.0000 | 0.0000 | -134.5778 | -1168.0484 | -1302.6175 | 0.0000 | 740.5334 | -562.0842 |
| 350 | -0.0149 | -0.0434 | -134.5902 | -1168.0918 | -1302.6718 | -0.0543 | 740.5874 | -562.0844 |
| 330 | -0.0827 | -0.2531 | -134.6510 | -1168.3015 | -1302.9333 | -0.3158 | 740.8477 | -562.0855 |
| 310 | -0.1360 | -0.1243 | -134.6682 | -1168.1727 | -1302.8076 | -0.1901 | 740.7220 | -562.0856 |
| 270 | -0.0957 | 0.6393 | -134.5876 | -1167.4091 | -1301.9436 | 0.6739 | 739.8610 | -562.0826 |

${ }^{a}$ The referential geometry for the calculations of the potential energies. The energies $E_{v}, E_{\mathrm{e}}$, and $E^{\mathrm{T}}$ were obtained from full SCF computation at the STO-3G level.
framework for the $d_{S H}=0.0 \AA$ geometry to be strongly stabilized by the QMRE. Benzene is $\sigma$ aromatic. ${ }^{30}$ On the other hand, the $\pi$ potential energy $R E_{\pi}^{(\pi, \sigma)}(0.0)=E_{\pi}^{(\pi, \sigma)}(0.0)-$ $E_{\pi}^{(\pi, \sigma)}(0.1644)$ is large, up to $20.6 \mathrm{kcal} / \mathrm{mol}$ (Table 8), revealing that the $\pi$-system of benzene is destabilized, and it prefers a distorted geometry. ${ }^{31}$

In the DSI state of benzene, the differences $d E_{\sigma}^{(\sigma)}\left(d_{S H}\right)=$ $E_{\sigma}^{(\sigma)}\left(d_{S H}\right)-E_{\sigma}^{(\sigma)}\left(d_{S H}^{0}\right)<0.0, d E_{\pi}^{(\sigma)}\left(d_{S H}\right)=E_{\pi}^{(\sigma)}\left(d_{S H}\right)-$ $E_{\pi}^{(\sigma)}\left(d^{0}{ }_{S H}\right)>0.0$ when $d_{S H}<d_{S H}^{0}$, and the absolute value of the $d E_{\sigma}^{(\sigma)}\left(d_{S H}\right)$ is less than that of the $d E_{\pi}^{(\sigma)}\left(d_{S H}\right)$. The $d E_{\sigma}^{(\sigma)}\left(d_{S H}\right)$ between the $d_{S H}=0.0$ and $0.1644 \AA$ geometries is, for example, $-24.359 \mathrm{kcal} / \mathrm{mol}$, and the corresponding $d E_{\pi}^{(\sigma)}\left(d_{S H}\right)$ is large up to $52.261 \mathrm{kcal} / \mathrm{mol}$. The $\sigma$-framework in the DSI state only possesses a distortive tendency. It is the $\pi$ delocalization to make this tendency become an effective driving force, expressed in terms of the $d E_{\sigma}^{(\pi, \sigma)}\left(d_{S H}\right)=\left[E_{\sigma}^{(\pi, \sigma)}\left(d_{S H}\right)-E_{\sigma}^{(\tau, \sigma)}\left(d_{S H}^{0}\right)\right]$ whose absolute value is now larger than that of the $d E_{\pi}^{(\pi, \sigma)}\left(d_{S H}\right)=$ $E_{\pi}^{(\pi, \sigma)}\left(d_{S H}\right)-E_{\pi}^{(\pi, \sigma)}\left(d_{S H}^{0}\right)$, for distorting the $d_{S H} \neq 0.0 \AA$ toward the symmetrical geometry. ${ }^{31}$ The $d E_{\sigma}^{(\pi, \sigma)}\left(d_{S H}=0.0\right)$ between the $d_{S H}=0.0$ and $0.1644 \AA$ geometries is, for example, -30.104 $\mathrm{kcal} / \mathrm{mol}$, and the corresponding $d E_{\pi}^{(\pi, \sigma)}(0.0)=20.603 \mathrm{kcal} /$ mol.

Table 9 shows further that in a given $d_{S H}$ geometry, the energy of the highest occupied MO (HOMO) of the $\pi$ type in the FUD state is always higher than that in the DSI state. Along the $d_{S H}$ distortion, the energy, about -0.27824 hartree, of the HOMO is highest at the $d_{S H}=0.0 \AA$ geometry. This energy character, together with those indicated by the $E_{\pi}^{(\pi, \sigma)}\left(d_{S H}\right)$ in Table 8 and
the $E_{\pi}^{(\pi, \sigma)}(\theta)$ in Table 6 , is in accordance with the chemical feature that the $\pi$ systems of benzene and STB-type 1 both are reactive toward electronphilic attack. However, the high stability of benzene due to the $\Delta E_{\sigma}^{\mathrm{Q}}(0.0)<0.0(-32.21 \mathrm{kcal} /$ mol ) is getting weaker while its $\pi$-system is increasingly localized under the electrophile attacking. In the transition state, the $\sigma$-framework of benzene is reluctant to undergo addition reaction and has to opt for "aromatic" substitution instead in order to maintain its original $\sigma$-aromaticity. On the other hand, STB-type $\mathbf{1}$ are willing to undergo addition reaction owing to their $\Delta E_{\sigma}^{\mathrm{Q}}(\theta)>0.0$. During the period of preparing $\mathbf{1 i}$, we found that the $-\mathrm{CH}=\mathrm{N}$ - double bond is very unstable in its alcohol solution; the addition product is 2-ethoxyl-2-(4-nitro-phenyl)- $N$-(2-pyrimidyl)ethylamine.
$\sigma$ Interaction Is a Main Driving Force for Out-of-Plane Twist. The electronic energy of the DSI state is the lowest of four hypothetical states. In this state, all the elements, such as $F_{i j}^{(\sigma)-\pi}, H_{i j}^{(\sigma)-\pi}$, and $D_{i j}^{(\sigma)-\pi}(i \neq j)$ corresponding to those in eqs (3-1)-(3-2), are equal to zero. Therefore, the potential energy, denoted as $R E_{\sigma}^{(\sigma)}(\theta)=E_{\sigma}^{(\sigma)}(\theta)-E_{\sigma}^{(\sigma)}\left(0^{\circ}\right)$, is useful for analyzing the molecular conformation. In the region of the $\theta$ from 0 to about $40^{\circ}$, the absolute values of the various energies in $\mathbf{1 h}$, such as the $E_{\sigma}^{(\sigma)}(\theta), E_{\mathrm{e}}(\theta)$ (Table 10), and $E_{\pi}^{(\pi)}(\theta)$ (Table 3), increase concurrently as the nuclear repulsion $E_{v}$ (Table 10) becomes larger. In a given conformer, the absolute value of $R E_{\sigma}^{(\sigma)}(\theta)$ is generally three times larger than that of the $R E_{\pi}^{(\pi)}(\theta)$, and it is very close to that of the $R E_{\mathrm{e}}(\theta)$. The

TABLE 11: Total $\sigma$-Electronic Energy $\boldsymbol{E}_{\sigma}^{(\boldsymbol{\sigma})}$ in the DSI States, Net $\sigma$-Electron Charge $D_{c}^{(\sigma)}$ and the Ratio, de/dv, of the $\boldsymbol{d} \boldsymbol{E}_{\sigma}^{(\sigma)}$ to $\boldsymbol{d} \boldsymbol{E}_{v}$ (Energy in Hartrees)

| $\theta$ (deg) | $E_{\sigma}^{(\sigma)}$ | $D_{c}^{(\sigma)}$ | $d e / d v$ |
| :---: | :---: | :---: | :---: |
| 1h |  |  |  |
| 0 | $-1168.0484$ | 0.10937 |  |
| 5 | -1168.0606 | 0.10951 | -0.82 |
| 1 i |  |  |  |
| 0 | -1606.5901 | 0.09159 |  |
| 5 | -1606.5965 | 0.09174 | -0.80 |
| 1 g |  |  |  |
| 0 | -1293.1949 | 0.10149 |  |
| 5 | -1293.1985 | 0.10158 | -0.78 |
| 1j |  |  |  |
| 0 | -1167.5517 | 0.12502 |  |
| 5 | -1167.5543 | 0.12515 | -0.82 |
| $1 f$ |  |  |  |
| 0 | -1589.1171 | 0.11283 |  |
| 5 | -1589.1206 | 0.11295 | -0.74 |
| 1e |  |  |  |
| 0 | -1754.9791 | 0.10945 |  |
| 5 | -1754.9830 | 0.10956 | -0.69 |

$R E_{\sigma}^{(\sigma)}$ plays a predominant role in determining the preferential geometry of $\mathbf{1 h}$.

In flexible molecules such as STB-type 1, it is difficult to determine which pair of the atoms makes the greatest contribution to the driving force. According to the definition $E_{v}=\Sigma_{i} \Sigma_{j-}$ $\left(e_{i} e_{j} / r_{i j}\right), E_{v}$ can be, indirectly, used to characterize the interaction distance between fragments, and the quantity $d e / d v$ in eq 7 can be defined as a generalized driving force for the out-of-plane twist.

$$
\begin{equation*}
d e / d v=\left[E_{\sigma}^{(\sigma)}\left(5^{\circ}\right)-E_{\sigma}^{(\sigma)}\left(0^{\circ}\right)\right] /\left[E_{v}\left(5^{\circ}\right)-E_{v}\left(0^{\circ}\right)\right] \tag{7}
\end{equation*}
$$

Comparison of the values of $d e / d v$ in Table 11 and those of the angle $\phi$ in Table 1 shows that a larger absolute value ( $>0.80$ ) of the $d e / d v$ corresponds to a larger twist angles $\phi\left(>30^{\circ}\right)$. The calculations for the net $\sigma$ electronic charge $D_{c}^{(\sigma)}(\theta)$ of fragment C (Table 11) show that, in the three typical molecules, the values of the $d D_{c}^{(\sigma)}=D_{c}^{(\sigma)}\left(5^{\circ}\right)-D_{c}^{(\sigma)}\left(0^{\circ}\right)$ are in the sequence: $1.5 \times$ $10^{-4}\left(1 \mathbf{i}\right.$ with a $-\mathrm{NO}_{2}$ group and two ring-nitrogen atoms) $>1.4$ $\times 10^{-4}(\mathbf{1 h}$ with a ring-nitrogen atom on fragment C$)>1.3 \times$ $10^{-4}(\mathbf{1} \mathbf{j}$ with a ring-nitrogen atom on fragment A$)$, and their respective values of the angle $\phi$ are $50(\mathbf{1 i})>38(\mathbf{1 h})>35^{\circ}$ $(\mathbf{1 j})$. It seems that the electron-withdrawing ( -I ) groups and the ring-nitrogen atoms have an obvious influence upon the twist angle.

## Summary

We have been successful in separating $\sigma$ from $\pi$ FMOs based on our new procedure. Besides the well-known resonance interaction between fragments, the $\sigma$-electron interaction, arising from the effect of the $\pi$-electron delocalization on the $\sigma-\pi$ space interactions, is also stabilization. However, the delocalization of the $\pi$-electrons in the DPI state not only reduces the original $\pi$ energies in fragments, but also the energy gains are insufficient to compensate for the energy loss. The $\pi$-electron delocalization in the DPI state is found to be destabilization. As a result, the DPI state is most destabilized at a coplanar geometry, and, in a given geometry, its electronic energy is highest of four hypothetical states. The characteristic of the QMRE depends upon the response of the $\sigma$ framework to the $\pi$ delocalization. In the case of stilbene-like species, the QMRE is destabilizing. On the other hand, the QMRE of benzene is stabilizing. However, it is the $\sigma$ framework, rather than the $\pi$ system itself, which is strongly stabilized by the QMRE, revealing that benzene is $\sigma$ aromatic.

Contrary to the viewpoints in the literature, the driving forces for the out-of-plane twist of stilbene-like species are due to the $\sigma$ orbital interaction and the QMRE. It seems that the electronwithdrawing ( -I ) groups on the aromatic ring and the ringnitrogen atoms, has an obvious influence on the twist angle.

## Experimental Section

General Methods. All starting materials were obtained commercially as reagent grade. Melting points were determined on a Nagoya apparatus and are uncollected. ${ }^{1} \mathrm{H}$ NMR spectra were recorded on a Varian Unity 200 NMR spectrometer. Crystal structures of molecules were determined by a Nicolet R3WE X-ray diffractometer. The crystal data of each of the following eight compounds are listed in Table 12.

N -(4-Chlorophenyl)methylene-2-pyridineamine (1e) was prepared from 4-chlorobenzaldehyde and 2-pyridineamine: ${ }^{32} \mathrm{mp}$ 96-99 ${ }^{\circ} \mathrm{C} ;{ }^{1} \mathrm{H}$ NMR $\left(\mathrm{CDCl}_{3}\right) 9.12(\mathrm{~s}, 1 \mathrm{H}), 8.56(\mathrm{~d}, 1 \mathrm{H}), 7.18-$ 7.92 (m, 7H).
$N$-(4-Nitrophenyl)methylene-2-pyridineamine (1f) was prepared from 4-nitrobenzaldehyde and N -(triphenylphosphora-nylidene)-2-pyridineamine: ${ }^{32} \mathrm{mp} 147-148{ }^{\circ} \mathrm{C}$; ${ }^{1} \mathrm{H}$ NMR $\left(\mathrm{CDCl}_{3}\right)$ $9.27(\mathrm{~s}, 1 \mathrm{H}), 8.58(\mathrm{~d}, 1 \mathrm{H}), 8.38-7.25(\mathrm{~m}, 7 \mathrm{H})$.
$N$-(4- $N, N$-Dimethylaminophenyl)methylene-2-pyridineamine (1g) was prepared from 4-N,N-dimethylbenzaldehyde and 2-pyridineamine: ${ }^{32} \mathrm{mp} 123-124{ }^{\circ} \mathrm{C} ;{ }^{1} \mathrm{H}$ NMR $\left(\mathrm{CDCl}_{3}\right) 9.1$ (s, $1 \mathrm{H}), 8.50(\mathrm{~d}, 1 \mathrm{H}), 7.9-6.8(\mathrm{~m}, 7 \mathrm{H}), 3.2(\mathrm{~s}, 6 \mathrm{H})$.

N -(4-Nitrophenyl)methylene-2-pyrimidineamine (1i) was prepared from 4-nitrobenzaldehyde and N -(triphenylphospho-

TABLE 12: Crystal Data of Four Stilbene-like Molecules 1 and Four Ketenimine Derivatives $\boldsymbol{2}^{\boldsymbol{a}}$

|  | 1e | $1 f$ | 1 g | 1i | 2 a | 2b | 2c | 2d |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| formula | $\mathrm{C}_{12} \mathrm{H}_{9} \mathrm{ClN}_{2}$ | $\mathrm{C}_{12} \mathrm{H}_{9} \mathrm{~N}_{3} \mathrm{O}_{2}$ | $\mathrm{C}_{14} \mathrm{H}_{15} \mathrm{~N}_{3}$ | $\mathrm{C}_{11} \mathrm{H}_{8} \mathrm{~N}_{4} \mathrm{O}_{2}$ | $\mathrm{C}_{20} \mathrm{H}_{15} \mathrm{~N}$ | $\mathrm{C}_{20} \mathrm{H}_{14} \mathrm{~N}_{2} \mathrm{O}_{2}$ | $\mathrm{C}_{22} \mathrm{H}_{18} \mathrm{~N}_{2} \mathrm{O}_{4}$ | $\mathrm{C}_{22} \mathrm{H}_{20} \mathrm{~N}_{2}$ |
| fw | 216.66 | 227.220 | 225.290 | 228.210 | 269.00 | 314.330 | 374.380 | 312.400 |
| color | colorless | yellow | yellow | yellow | yellow | red |  | yellow |
| $a$ | 6.509 | 7.096 | 11.923 | 6.015 | 20.594 | 7.972 | 13.439 | 9.919 |
| $b$ | 8.005 | 28.754 | 17.914 | 13.393 | 8.753 | 18.951 | 9.429 | 12.838 |
| c | 20.383 | 10.969 | 12.059 | 25.572 | 17.471 | 11.062 | 15.099 | 14.010 |
| $\alpha$ | 90.000 | 90.000 | 90.000 | 90.000 | 90.000 | 90.000 | 90.000 | 90.000 |
| $\beta$ | 98.270 | 106.500 | 103.990 | 90.000 | 101.698 | 106.911 | 93.171 | 90.000 |
| $\gamma$ | 90.000 | 90.000 | 90.000 | 90.000 | 90.000 | 90.000 | 90.000 | 90.000 |
| $U$ | 1051.000 | 2145.9 | 2499.300 | 2060.100 | 3083.900 | 1598.900 | 1910.400 | 1785.000 |
| $D_{\text {x }}$ | 1.369 | 1.407 | 1.197 | 1.472 | 1.158 | 1.306 | 1.302 | 1.162 |
| Z | 4 | 8 | 8 | 8 | 8 | 4 | 4 | 4 |
| absorp coeff | 0.328 | 0.100 | 0.073 | 0.107 |  | 0.086 | 0.091 | 0.064 |
| space group | $P 2_{1} / n$ | $P 2_{1}$ | $P 2{ }_{1} / c$ | Pca2 ${ }_{1}$ | C2/c | $P 2{ }_{1} / n$ | $P 2{ }_{1} / n$ | $P 2{ }_{1}{ }_{1} 2_{1}$ |

[^1]ranylidene)-2-pyrimidineamine: ${ }^{32} \mathrm{mp} 236-238{ }^{\circ} \mathrm{C} ;{ }^{1} \mathrm{H}$ NMR $\left(\mathrm{CDCl}_{3}\right) 9.33$ (s, H), 8.84 (d, 2H), 7.29-8.40 (m, 6H).

N -(Diphenylethenylidene)benzeneamine (2a) was obtained as bright yellow crystalline from phenyl isocyanate and (diphenylmethylene)triphenylphosphorane: $:^{33} \mathrm{mp} 55-56{ }^{\circ} \mathrm{C}$; ${ }^{1} \mathrm{H}$ NMR $\left(\mathrm{CDCl}_{3}\right)$ 7.32-7.40 (m, Ar-H).

N -(Diphenylethenylidene)-4-nitrobenzeneamine (2b) was obtained as a red crystal from triphenylphosphine, bromine, triethylamine, and $N$-(4-nitrophenyl)diphenylacetamide: ${ }^{34} \mathrm{mp}$ $84-86{ }^{\circ} \mathrm{C} ;{ }^{1} \mathrm{H}$ NMR $\left(\mathrm{CDCl}_{3}\right) 8.27(\mathrm{~d}, 2 \mathrm{H}), 7.45(\mathrm{~d}, 2 \mathrm{H}), 7.28-$ 7.40 (m, 10H).
$N$-(Bis(4-methoxyphenyl)ethenylidene)-4-nitrobenzeneamine (2c) was obtained using the same procedure for preparing 2a. It was obtained as red crystals: mp $103.5-105.5{ }^{\circ} \mathrm{C}$; ${ }^{1} \mathrm{H}$ NMR ( $\mathrm{CDCl}_{3}$ ) 6.92, $7.24(2 \mathrm{~d}, 8 \mathrm{H}), 7.44,8.26(2 \mathrm{~d}, 4 \mathrm{H}), 3.82$ ( $\mathrm{s}, 6 \mathrm{H}$ ).
$N$-(Diphenylethenylidene)-4-( $N, N$-dimethylamino)benzeneamine (2d) was obtained using the same procedure for preparing 2a. It was obtained as yellow crystals: mp $90-92^{\circ} \mathrm{C} ;{ }^{1} \mathrm{H}$ NMR $\left(\mathrm{CDCl}_{3}\right) 6.69(\mathrm{~d}, 2 \mathrm{H}), 7.20-7.36(12 \mathrm{H}, \mathrm{m}), 2.98(\mathrm{~s}, 6 \mathrm{H})$.

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[^1]:    ${ }^{a}$ Units: $\alpha, \beta$, and $\gamma, \operatorname{deg} ; U, \AA^{3} ; D_{\mathrm{x}}, \mathrm{g} / \mathrm{cm}^{3} ;$ absorption coefficient, $\mathrm{cm}^{-1}$.

