# Conformations of Stilbene-like Species and New Method of Energy Partition

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To understand the nature of  $\pi$ -electron delocalization, while questioning the abnormally large twist angle of *N*-benzylideneaniline, we prepared four stilbene-like species, (4-X-Ph)-CH=N-Ar (Ar = 2-pyridyl, X = -Cl,  $-NO_2$ ,  $-N(Me)_2$ ; Ar = 2-pyrimidyl, X =  $-NO_2$ ), and four ketenimine derivatives,  $(4-X-Ph)_2C=C=N-(Ph-Y-4)$  $(Y = -H, X = -H; Y = -NO_2, X = -H; Y = -NO_2, X = -OMe; Y = -N(Me)_2, X = -H)$ , and determined their crystal structures using X-ray diffraction. Our new procedure for constructing a complete fragment molecular orbital (FMO) basis set is described in detail. Based on our procedure, the Morokuma's energy partitioning provides, in the framework of ab initio SCF-MO computation at the STO-3G level, the various  $\pi$  and  $\sigma$ energies associated with the inter- and intrafragment interactions. The  $\pi$ -electron delocalization in the DPI state of stilbene-like species is found to be destabilization. The DPI state is most destabilized at the coplanar geometry, and its electronic energy is the highest of four hypothetical electronic states. The characteristics of the quantum mechanical resonance energy (OMRE), including its role with regard to chemical reactivities toward electrophile attack, depend upon the response of the  $\sigma$  framework to the  $\pi$ -electron delocalization. In the case of stilbene-like species, the QMRE is destabilizing. Conversely, the QMRE of benzene is stabilizing. However, it is the  $\sigma$  framework of benzene, rather than the  $\pi$  system itself, which is strongly stabilized by the QMRE, revealing that benzene is  $\sigma$  aromatic. The driving forces for the out-of-plane twist of stilbene-like species arise from the QMRE and the  $\sigma$  orbital interaction. The electron-withdrawing (-I) groups and the ring-nitrogen atoms seem to have an obvious influence upon the twist angle.

## Introduction

It has been recognized as a cornerstone of the classical structure theory of organic chemistry that molecules with conjugated double bonds have a higher thermodynamic stability than isomeric compounds having isolated double bonds. The standard textbook explanation for this stability is given in terms of resonance interactions.<sup>1</sup> It is also one of the fundamental concepts that the maximum resonance energy results from the planarity of the  $\pi$  system.<sup>1,2</sup> However, the abnormally large twist angle of stilbene-like species seems to challenge the viewpoint of  $\pi$  resonance stabilization.

The marked dissimilarity in the electronic spectra of stilbene (STB, 1a) and N-benzylideneaniline (NBA) has led to many theoretical and experimental studies and arguments in the past two or three decades, including studies employing infrared (IR) and a variety of nuclear magnetic resonance (NMR) studies, X-ray crystallography, and molecular orbital calculations.<sup>3</sup> The resonance stabilization is always used to interpret the effects of substituents on the conformations of NBA and its substituted derivatives.<sup>4</sup> Burgi and recent researchers ascribed the large twist angle ( $\phi = 55^{\circ}$ ) of NBA to the contact of nonbonded atoms such as the hydrogen on the -N=CH- and one of the ortho hydrogens on the aniline ring. The loss of the  $\pi$ -electron energy in the twisted geometry can be compensated for partly by the intramolecular charge transfer (CT-2) from the bridge nitrogen lone-pair electrons to the phenyl ring and by the decrease in steric hindrance;<sup>5</sup> these researchers expected, therefore, that if the nonbonded interaction was neglected, the  $\pi$ -electron transfer (CT-1) between the conjugated fragments was found to favor the planar conformation of NBA.<sup>6</sup> Burgi's conclusions appear to be questioned by the angles  $\phi$  of stilbene-like species, especially by those (both up to 30°) of **1a** and azobenzene (**1d**) in the gas state,<sup>7</sup> and by those of the compounds listed in Table 1. (The phrase "stilbene-like species listed in Table 1" or "the molecules of type **1**" is often, hereafter, shortened to "STB-type **1**".)

In order to discern whether conjugation effect depends on conformation or results in a nonplanar geometry, we prepared the following eight compounds with less nonbonded contact such as that in NBA: (4-X-Ph)-CH=N-2-pyridyl (1e, X = -Cl; 1f,  $X = -NO_2$ ; 1g,  $X = (Me)_2N$ -), 4-NO<sub>2</sub>-Ph-CH=N-2-pyrimidyl (1i) and (4-X-Ph)<sub>2</sub>C=C=N-(Ph-Y-4) (2a, X = -H, Y = -H; 2b, X = -H,  $Y = -NO_2$ ; 2c, X = -MeO,  $Y = -NO_2$ ; 2d, X = -H,  $Y = -N(Me)_2$ ) and determined their crystal structures using X-ray diffraction (see Table 1 and Figures 1–3).

The total molecular energies  $E^{\rm T}$ , total electronic energies  $E_{\rm e}$ , and total nuclear repulsion energies  $E_{\rm N}$ , occurring in seven typical optimized geometries of each of seven STB-type 1 were calculated using the AM1 method.<sup>12</sup> In addition, the nuclear repulsion energies  $E_n$  between the aromatic ring and fragment Ar-Q=P- were obtained from the ab initio SCF-MO (selfconsistent field molecular orbital) program. The nonbonded contact in 1e-1g and 1i (Figure 1) should be comparable to that in 2a-2d (Figure 2), but the twist angles  $\phi$  for the former are generally larger than those for the latter. Of all the molecules listed in Table 1, the theoretical angle ( $\phi = 50^{\circ}$ ) of **1i** is largest and the experimental angle ( $\phi = 0.5^{\circ}$ ) of **2a** is smallest. The data in Table 2 are especially noteworthy. These data show identically that the driving force for out-of-plane twist of STB-type 1 arises from the electron interaction, expressed in terms of  $E_{\rm e}$ , rather than from the nuclear repulsion  $E_{\rm N}$  and  $E_{\rm n}$ . At the  $\theta = 30^{\circ}$  geometry of **1h**, for example, the absolute

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TABLE 1: Experimental and Theoretical Values (deg) of Twist Angles  $\phi$  and  $\alpha$  in Compounds of Types 1 and 2



									twist a	ngle $\phi$	twist a	ngle α
compd	Р	Q	Х	Y	Ζ	W	R	R′	X-ray	AM1	X-ray	AM1
<b>1</b> a	CH	CH	CH	CH	СН	С	Н	Н	$5^a$	27	5	27
1b	Ν	CH	CH	CH	CH	С	$N(Me)_2$	$NO_2$	$41^{b}$	40	10	0
1c	Ν	CH	CH	CH	CH	С	$NO_2$	$N(Me)_2$	$9^b$	$15^{e}$	4	0
1d	Ν	Ν	CH	CH	CH	С	Н	Н	$15^{c}$	15	15	15
1e	Ν	CH	Ν	CH	CH	С	Cl	Н	15	13	6	3
1f	Ν	CH	Ν	CH	CH	С	$NO_2$	Н	20	0	2	0.5
1g	Ν	CH	Ν	CH	CH	С	N(Me) <sub>2</sub>	Н	36	$15^{e}$	7	0
1ĥ	Ν	CH	CH	CH	Ν	С	Н	Н	$46^{d}$	38	13.4	14
1i	Ν	CH	Ν	Ν	CH	С	$NO_2$	Н	26	50	12	4.5
1j	Ν	CH	CH	CH	CH	Ν		Н	$21^d$	$35^e$	8	2
2a							Н	Н	0.5			
2b							$NO_2$	Н	16			
2c							$NO_2$	MeO	6.5			
2d							N(Me) <sub>2</sub>	Н	9.1			

<sup>a</sup> This value is from ref 8. <sup>b</sup> From ref 9. <sup>c</sup> From ref 10. <sup>d</sup> From ref 11. <sup>e</sup> Conformational space was sampled by varying  $\theta$  in steps of 5°.

value ( $|-11\ 090.9611|eV$ ) of  $E_e$  and value (9004.6837 eV) of  $E_{\rm N}$  are greatest, and decrease as the molecular framework is distorted away from this geometry. Therefore, we cannot attribute the nonplanarity of STB-type 1 to the steric hindrance or to the crystal lattice force.<sup>13</sup> In molecule 2c (Figure 2), the combination of the "pushing" and "pulling" actions, exerted by an electron-releasing (+M) group MeO- and an electronwithdrawing (-M) group  $-NO_2$ , respectively, should greatly benefit the CT-2 interaction between the nitrogen lone pair and phenyl ring A, and its twist angle  $C_8-N_7-C_1-C_6$  should be larger than the angle  $(41^{\circ})$  in **1b**. At the least, it should be larger than that (16°) in 2b. Contrary to expectation, the actual angle is only 9.2°. Nakai and collaborators found that the C1- $N_7$  distance in several molecules such as 1c (1.416 Å) and 1b (1.398 Å) decreases with increasing CT-2 effect.<sup>9</sup> Accordingly, this distance should decrease in order of 1f, 1i, and 1g and of 2d, 2a, 2b, and 2c, respectively. In fact, the bond length (1.439 Å) in **1i** is much longer than that (1.410 Å) in **1f**, and the experimental value (1.409 Å) in 1g is almost equal to that in 1f (Figure 1); of the four ketenimine derivatives, the distance (1.436 Å) in **2a** is longest and that (1.419 Å) in **2d** is shortest (Figure 2). Recently, our calculations have approximately shown that in the aniline molecule, the CT-2 interaction is destabilizing.<sup>14</sup> Accordingly, the nonplanarity of STB-type 1 cannot be explained in terms of the CT-2.

In this work, our procedure for constructing a complete fragment molecular orbital (FMO) basis set is described in detail. Morokuma's partition of the intermolecular SCF interaction energy,<sup>15</sup> denoted as M-SCF partition, is introduced into the intramolecular interaction, and it is used for analyzing the direct and indirect effects of the  $\pi$ -electron delocalization, respectively, on the  $\pi$  system itself and the  $\sigma$  frame in an effort to gain insight into the nature of the  $\pi$ -electron delocalization. Meanwhile, it is also applied to the  $\sigma$  interactions in order to search for the unknown driving force and to probe the influence of the electron-withdrawing (-I) effect upon the twist angle.

## Methods and Computational Details

Based on the most common definitions of the resonance energy (RE),<sup>16</sup> the RE is essentially associated with the local interaction between double bonds. Inevitably, this interaction influences the original characteristics of the double bonds, including the observed and calculable changes in their bond lengths and bond orders, and also including the disturbance to their original  $\pi$  energies.<sup>17</sup> The geometric data in Figure 3, for example, indicate that the lengths of the bonds N<sub>7</sub>-C<sub>8</sub> and C<sub>1</sub>- $C_6$  are changed as the bond  $C_1$ - $N_7$  is lengthened from 1.405 to 1.411 Å with the rotation of fragment A about the  $C_1 - N_7$ . Accordingly, the fundamental problems in the energy partitioning are how to calculate, reasonably and directly, the  $\pi$  energies occurring in a conjugated molecule and its corresponding hypothetical structures with the localized  $\pi$  systems, and how to evaluate the effects of the  $\pi$ -electron delocalization on the  $\sigma$ framework. In this sense, the perturbation molecular orbital (PMO) method should be more reasonable and valuable. It is prerequisite for the PMO analysis that the symmetric ( $\sigma$ ) and antisymmetric ( $\pi$ ) FMOs are thoroughly separated. It is easy when and only when the geometry of a molecule is planar.<sup>18</sup> However, STB-type 1 are not planar. In this case, the M-SCF method based on our new procedure becomes a useful instrument for partitioning total electronic energy. Our procedure provides a complete FMO basis set for the M-SCF partition.

According to the PMO theory<sup>19</sup> and based on the fact that in STB-type **1** both twist angles  $\phi$  and  $\alpha$  are not equal to 0° or 180°, we can consider a nonplanar molecule *N*-phenylmethylene-3-pyridineamine (**1h**), for example, as three planar openedshell fragments, phenyl fragment (A), imine group -CH=N- (B), and 3-pyridyl fragment (C), i.e., A-B-C dissection as shown in Figure 4.

Figure 5 displays a thermodynamic cycle for the orbital interactions in STB-type 1. It shows the symbols for the  $\pi$ -and  $\sigma$ -electronic energies in the following hypothetical states: the full localized state denoted as FUL; the state, denoted as DPI, with a delocalized  $\pi$  system and localized  $\sigma$  frameworks;



Figure 1. Experimental and theoretical geometric data of four stilbene-like molecules.

the DSI state with delocalized  $\sigma$  frameworks and localized  $\pi$  systems; the full delocalized state denoted as FUD. Figure 5 also contains a set of definitions of the various energy differences that will be used consistently in this work. For simplicity, these energy differences are expressed by the following general formulas:

$$\Delta E_{\pi}^{(\lambda,\rho)} = \Delta E_{ab+bc+ca}^{(\lambda,\rho)-\pi} + \Delta E_{a+b+c}^{(\lambda,\rho)-\pi}$$
(1-1)

$$\Delta E_{\sigma}^{(\lambda,\rho)} = \Delta E_{ab+bc+ca}^{(\lambda,\rho)-\sigma} + \Delta E_{a+b+c}^{(\lambda,\rho)-\sigma}$$
(1-2)

where the characters  $\lambda$  and  $\rho$  ( $\lambda$ ,  $\rho = \pi$ ,  $\sigma$ ) in the superscript

 $(\lambda,\rho)$  mean that the energy effects  $\Delta E_{\pi}^{(\lambda,\rho)}$  and  $\Delta E_{\sigma}^{(\lambda,\rho)}$  arise from the delocalization of the  $\lambda$ - and  $\rho$ -electrons; the characters  $\pi$ and  $\sigma$  in super- and subscripts denote that the energy effects are associated, respectively, with the  $\pi$  and  $\sigma$  orbital interactions. When  $\lambda = \pi$  and  $\rho = \pi$ , eqs (1-1) and (1-2) become

$$\Delta E_{\pi}^{(\pi)} = \Delta E_{ab+bc+ca}^{(\pi)-\pi} + \Delta E_{a+b+c}^{(\pi)-\pi}$$
(2-1)

$$\Delta E_{\sigma}^{(\pi)} = \Delta E_{ab+bc+ca}^{(\pi)-\sigma} + \Delta E_{a+b+c}^{(\pi)-\sigma}$$
(2-2)

where  $\Delta E_{\pi}^{(\pi)}$  and  $\Delta E_{\sigma}^{(\pi)}$  are the energy differences between the DPI and FUL states. Two terms in the right side of eq (2-1)



Figure 2. Crystallographic data of four ketenimine derivatives.

are the energy components associated, respectively, with the inter- and intrafragment interactions, and are given as

$$\Delta E_{ab+bc+cb}^{(\pi)-\pi} = \Delta E_{ab}^{(\pi)-\pi} + \Delta E_{bc}^{(\pi)-\pi} + \Delta E_{ca}^{(\pi)-\pi}$$
(2-3)

$$\Delta E_{a+b+c}^{(\pi)-\pi} = \Delta E_{a}^{(\pi)-\pi} + \Delta E_{b}^{(\pi)-\pi} + \Delta E_{c}^{(\pi)-\pi}$$
(2-4)

where

$$\Delta E_a^{(\pi)} = E_a^{(\pi)-\pi} - E_a^{(o)-\pi}, \ \Delta E_b^{(\pi)} = E_b^{(\pi)-\pi} - E_b^{(o)-\pi}, \ \Delta E_c^{(\pi)} = E_c^{(\pi)-\pi} - E_c^{(o)-\pi}$$
(2-5)

In the case of STB-type 1,  $|\Delta E_{ac}^{(\pi)-\pi}| < 10^{-3}$ ; hence, eq (2-3) is

often written as

$$\Delta E_{ab+bc}^{(\pi)-\pi} = \Delta E_{ab}^{(\pi)-\pi} + \Delta E_{bc}^{(\pi)-\pi}$$
(2-6)

In this work, the energy components such as those in eqs (2-3)-(2-6) are often written as the general forms  $\Delta E_{pq}^{(\pi)-\lambda}$  and  $\Delta E_p^{(\pi)-\lambda}$  where  $p, q = a, b, c; p \neq q; \lambda = \pi, \sigma$ ). In this case, the subscript pq and the character  $\lambda$  in the superscript  $(\pi)-\lambda$  mean that the  $\Delta E_{pq}^{(\pi)-\lambda}$  is associated with the  $\lambda$  orbital interactions between fragment P and Q (P, Q = A, B, C; P  $\neq$  Q), and the subscript p denotes a energy effect  $\Delta E_p^{(\pi)-\lambda}$  occurring in fragment P. In eq (2-5), the character  $\sigma$  in the superscript ( $\sigma$ ) is a  $\lambda$  electronic

TABLE 2: Total Molecular Energy  $E^{T}$ , Total Electronic Energy  $E_{e}$ , Total Nuclear Repulsion  $E_{N}$ , Nuclear Repulsion  $E_{n}$ (hartrees) between Fragments C and A + B, and Their Changes with Rotation of Fragment C (Energy in eV except for  $E_{n}$ )<sup>*a*</sup>

			,	8			I II
	$\theta = 0^{\circ}$	$\theta = 5^{\circ}$	$\theta = 10^{\circ}$	$\theta = 30^{\circ}$	$\theta = 50^{\circ}$	$\theta = 70^{\circ}$	$\theta = 90^{\circ}$
				1a			
$E^{\mathrm{T}}$	-1 956.3956	-1 956.3965	-1 956.3988	-1 956.4010	-1 956.3544		
$E_{\rm e}$	-10866.6455	-10867.0250	-10868.0638	-10874.0003	-10 871.0929		
$E_{\rm N}$	8 910.2499	8 910.6289	8 911.6649	8 917.5993	8 914.7384		
$E_{n}$	229.3696	229.3942	229.4682	229.9104	229.8220		
				1b			
$E^{\mathrm{T}}$	-3 383.8153	-3383.8150	-3 383.8191	-3 383.8376	-3 383.8378	-3 383.8211	
$E_{\rm e}$	-20 354.9945	-20 355.6694	-20 356.3679	-20 362.3796	$-20\ 360.1906$	-20 351.4668	
$E_{\rm N}$	16 971.1792	16 971.8534	16 972.5488	16 978.5420	16 976.3527	16 967.6457	
$E_{n}$	381.1377	381.1843	381.2470	381.7394	381.5754	380.8868	
				1d			
$E^{\mathrm{T}}$	$-2\ 085.5479$	$-2\ 085.5481$	$-2\ 085.5484$	$-2\ 085.5425$	$-2\ 085.5071$	-2085.4587	$-2\ 085.4424$
$E_{\rm e}$	-11 110.8509	-11 110.8661	-11 110.9009	-11 111.6857	-11 111.8174	-11 108.9611	-11 107.4265
$E_{\rm N}$	9 025.3029	9 025.3181	9 025.3525	9 026.1432	9 026.3103	9 023.5024	9 021.9545
$E_{\rm n}$	237.0091	237.0092	237.0093	237.0371	237.0132	236.8095	236.6407
				1e			
$E^{\mathrm{T}}$	-2446.2838	-2 446.2839	-2446.2841	-2446.2803	-2 446.2559	-2446.2068	
$E_{\rm e}$	-12 559.3338	-12 559.3430	-12 559.5186	-12 560.4603	-12 560.3311	-12 557.6144	
$E_{\rm N}$	10 113.0499	10 113.0591	10 113.2345	10 114.1800	10 114.0752	10 111.4076	
$E_{n}$	272.0361	272.0402	272.0553	272.1561	272.1461	271.8893	
				1f			
$E^{\mathrm{T}}$	-2 917.0114	-2917.0114	-2 917.0113	-2917.0062	-2 916.9803		
$E_{ m e}$	-15 549.8119	-15 549.8462	-15 549.9552	-15 551.1046	-15 551.0171		
$E_{\rm N}$	12 632.8005	12 632.8348	12 632.9439	12 634.0984	12 634.0368		
$E_{n}$	284.5411	284.5444	284.5526	284.6605	284.6523		
				1h			
$E^{\mathrm{T}}$	-2086.2632	-2086.2643	-2086.2665	-2086.2773	2 086.2675	-2086.2417	-2086.2269
$E_{\rm e}$	-11 087.7973	-11 087.8483	-11 088.1340	-11 090.9611	-11 089.0204	-11 082.1533	-11 078.3659
$E_{\rm N}$	9 001.5341	9 001.5840	9 001.8675	9 004.6837	9 002.7529	8 995.9116	8 992.1390
$E_{n}$	235.6215	235.6290	235.6588	235.9209	235.7749	235.1954	234.8701
				1i			
$E^{\mathrm{T}}$	-2 981.5947	-2 981.5953	-2 981.5982	-2 981.6182	-2 981.6315		
$E_{\rm e}$	-15 656.0401	-15 656.1216	-15 656.2985	-15 658.3358	-15 658.4500		
$E_{\rm N}$	12 674.4455	12 674.5263	12 674.6976	12 676.7176	12 676.8184		
$E_{n}$	286.1286	286.1398	286.1591	286.3514	286.3859		

<sup>*a*</sup> The starting geometry of each molecular conformation was taken from its crystal structure. The conformational space was sampled by varying  $\theta$  in steps of 5° for 0° <  $\theta$  < 90°. At each point a full optimization was carried out under the condition that all the ring atoms in each of two aromatic ring were kept coplanar.

energy in the FUL state of fragment P. In eq (2-2), the energy effect  $\Delta E_{\sigma}^{(\pi)}$  is the response of the  $\sigma$  framework to the delocalization of the  $\pi$ -electrons and it arises from the effects of the  $\pi$ -electron delocalization on the  $\sigma$ - $\pi$  space interactions expressed in terms of the Coulomb  $J_{\sigma\pi}$  and exchange  $K_{\sigma\pi}$ integrals. In the M-SCF scheme, the energy components  $\Delta E_{pq}^{(\pi)-\lambda}$  and  $\Delta E_p^{(\pi)-\lambda}$  are obtained from the following general expressions:

$$\Delta E_{pq}^{(\pi)-\lambda} = \sum_{i,j}^{\lambda} (F_{ij}^{(\pi)-\lambda} + H_{ij}^{(\pi)-\lambda}) D_{ij}^{(\pi)-\lambda} \quad i \in \mathbf{P}, j \in \mathbf{Q}$$
(3-1)

$$E_p^{(\pi)-\lambda} = \sum_{i,k}^{\lambda} (F_{ik}^{(\pi)-\lambda} + H_{ik}^{(\pi)-\lambda}) D_{ik}^{(\pi)-\lambda} \quad i, k \in \mathbb{P} \quad (3-2)$$

$$E_{p}^{(0)-\lambda} = \sum_{i,k}^{\lambda} (F_{ik}^{(0)-\lambda} + H_{ik}^{(0)-\lambda}) D_{ik}^{(0)-\lambda} \quad i,k \in \mathbb{P}$$
 (3-3)

where **F**, **H**, and **D** are Fock, Hamiltonian, and density matrices respectively (a capital bold letter denotes, hereafter, a matrix over the complete FMO basis set);  $F_{ij}^{(\pi)-\lambda}$ ,  $H_{ij}^{(\pi)-\lambda}$ ,  $D_{ij}^{(\pi)-\lambda}$  et al. are their respective elements. The various elements in eqs (3-1)–(3-2) are obtained from the RHF (restricted Hartree–Fock) computation, denoted as RHF<sup> $\pi$ </sup>-m in Figure 5,

for the DPI state under the following conditions: in each SCF iteration, all the elements  $S_{ii}$  (the elements of the overlap integral matrix **S**) and  $F_{ij}$  ( $i \neq j$ ) between the FMOs of the  $\sigma$  type are set equal to zero except four elements,  $F_{sa,sb1}$ ,  $S_{sa,sb1}$ ,  $F_{sc,sb2}$ , and  $S_{sc,sb2}$ . The subscripts sa and sb1 in  $F_{sa,sb1}$  denote a pair of the singly occupied FMOs belonging, respectively, to two bonded fragments A and B, and the sc and sb2 (sb1  $\neq$  sb2) a pair of those belonging to fragments C and B. The conditional RHF computation, denoted as RHF<sup> $\pi$ </sup>-f, for the various elements in eq (3-3) was performed over the same complete FMO basis. In this computation, all the elements  $S_{ij} = 0.0$  and  $F_{ij} = 0.0$  ( $i \neq$ *j*) except the elements  $F_{sa,sb1}$ ,  $S_{sa,sb1}$ ,  $F_{sc,sb2}$ , and  $S_{sc,sb2}$ . In the conditional RHF computation, denoted as RHF<sup> $\sigma$ </sup>-m, for the various elements in the DSI state, all the  $F_{ij}$  and  $S_{ij}$   $(i \neq j)$ between the FMOs of the  $\pi$  type are set equal to zero. The RHF-T computation for the elements, such as  $F_{ij}^{(\sigma,\pi)-\lambda}$ ,  $H_{ij}^{(\sigma,\pi)-\lambda}$ , and  $D_{ij}^{(\sigma,\pi)-\lambda}$ , in the FUD state was performed under the constraint, a fundamental requirement for every type of conditional RHF computation, that all the  $F_{ij}$  and  $S_{ij}$  between the  $\pi$  and  $\sigma$  FMOs are set equal to zero. All the conditions employed in each of four types of the conditional RHF computations ensure that the molecular orbitals (MOs) of the  $\pi$  type are thoroughly separated from those of the  $\sigma$  type.

The complete FMO basis set, in which all FMOs have correct electron occupancies, consists of CDF-MOs (closed-shell de-



Figure 3. The crystal structure of 1h, and its rotational geometries 1h-R0, 1h-R40, 1h-R90, 1h-PL, and 1h-VER obtained from AM1.

localized FMOs) and singly occupied OLF-MOs (opened-shell localized FMOs). The construction of this basis set is a threestep procedure: (i) three basis sets from their respective planar fragment molecules (PFM), (ii) transformation of the basis set for the PFM into that for the corresponding nonplanar fragment molecule, and (iii) the formation of a complete basis set for the optimized geometry of a molecule by the superposition of three basis sets belonging, respectively, to fragments A, B, and C.

**Construction of a Complete FMO Basis Set.** According to the Whangbo–Schlegel–Wolfe–Kost (WSW-K) procedure,<sup>20</sup> i.e., a conditional UHF (unrestricted Hartree–Fock) computation for the composite system such as **1h** followed by the Kost's localization, three groups of OLF-MOs can be characterized by the following expressions:

$$\psi_{ai} = \sum_{k=1}^{na} a_{ki} \phi_k + \sum_{m=na+1}^{na+nb} a_{mi} \phi_m + \sum_{n=na+nb+1}^{N} a_{ni} \phi_n \quad (4-1)$$

$$\psi_{bj} = \sum_{k=1}^{na} a_{kj} \phi_k + \sum_{m=na+1}^{na+nb} a_{mj} \phi_m + \sum_{n=na+nb+1}^{N} a_{nj} \phi_n \quad (4-2)$$

$$\psi_{cl} = \sum_{k=1}^{na} a_{kl} \phi_k + \sum_{m=na+1}^{na+nb} a_{ml} \phi_m + \sum_{n=na+nb+1}^{N} a_{nl} \phi_n \quad (4-3)$$

where the atomic orbitals (AOs)  $\phi_k$  ( $k = 1, 2, ..., n_a$ )  $\in A, \phi_m$  $(m = n_a + 1, ..., n_a + n_b) \in B$ , and  $\phi_n (n = n_a + n_b + 1, ..., N)$  $\in$  C;  $a_{ki}$ ,  $a_{mi}$ , and  $a_{ni}$  are their coefficients. In our new procedure, the first sum term in eq (4-1), i.e., a set of the OLF-MOs  $\psi_{ai}$ for the isolated fragment A, is obtained indirectly from a planar fragment molecule, denoted as FM-A in Figure 4b, using the WSW-K procedure. The FM-A resulted from the replacement of the 3-pyridyl-N=CH- group (B + C) in **1h** with a hydrogen atom denoted as H<sub>r</sub> while all the bond angles and bond lengths were kept unchanged with the exceptions that the value of 1.0 Å was imposed on the length of the  $C_9-H_r$  bond and the dihedral angle  $H_r-C_9-C_{10}-C_{11}$  was set equal to 180°. The 1s AO of the H<sub>r</sub>, denoted as  $\psi_{\rm H}$ , is an excellent singly occupied  $\sigma$ FMO, and the formation of the FM-A simplifies the localization procedure greatly. However, the dihedral angles, such as the  $C_8-C_9-C_{10}-C_{11}$  and  $N_7-C_1-C_2-C_3$  in Figures 1 and 3, are generally less than 180°. Therefore, it is necessary for the OLF-MOs of the  $\sigma$  type to be localized once more. In the second



(b)

**Figure 4.** (a) The dissection way and the numbering system in *N*-phenylmethylene-3-pyridineamine (**1h**). The A-B-C dissection of **1h** into a phenyl fragment (A), an imine group (B), and a 3-pyridyl fragment (C). (b) Formation of the corresponding fragment molecules denoted as FM-A, FM-B, and FM-C.

localization, all the  $\pi$  OLF-MOs are kept unchanged, and the atomic overlap integral matrix **s** used in Kost's localization is from a nonplanar fragment molecule denoted as NFM-A. The only difference in the geometry between the FM-A and the NFM-A occurs in the angle H<sub>r</sub>-C<sub>9</sub>-C<sub>10</sub>-C<sub>11</sub>. In the case of the NFM-A, this angle is set equal to the C<sub>8</sub>-C<sub>9</sub>-C<sub>10</sub>-C<sub>11</sub> in the optimized geometry of **1h**.

However, the Kost's localization fails to ensure all the  $\pi$  OLF-MOs correct electronic occupancies. A conditional RHF computation, over the OLF-MOs basis set, for the NFM-A has to be performed after the Kost's localization. From this computation, a set of the CDF-MOs  $\varphi_{ai}$  is obtained under the following conditions: first, all the elements  $F_{ij} = 0.0$  and  $S_{ij} =$ 0.0 ( $i \in A, j \in H_r$ ) except two elements  $F_{sa,H}$  and  $S_{sa,H}$  between a pair of singly occupied OLF-MO  $\psi_{sa}$  and  $\psi_{H}$ ; second, all the intrafragment elements  $F_{sa,ai}$  and  $S_{sa,ai}$  (sa  $\neq$  ai) and those between the  $\pi$  and  $\sigma$  OLF-MOs are set equal to zero. A set of the CDF-MOs and a singly occupied OLF-MO  $\psi_{sa}$  form a FMO basis set  $\Phi_{ai}$  for fragment A. All  $\Phi_{ai}$  have now correct electronic occupancies, and the  $\pi$  type of  $\Phi_{ai}$  has been thoroughly separated from the  $\sigma$  type. A FMO basis set  $\Phi_{bi}$ for fragment B and that  $\Phi_{cl}$  for fragment C are obtained in a similar way. In the case of fragment B, there are two singly occupied OLF-MOs  $\psi_{sb1}$  and  $\psi_{sb2}$ . A singly occupied OLF-MO for fragment C is denoted as  $\psi_{sc}$ . At last, according to the characteristics as shown in eqs (4-1)-(4-3), a complete FMO basis set is formed by the superposition of three basis sets,  $\Phi_{ai}$ ,  $\Phi_{bj}$ , and  $\Phi_{cl}$ . In the meantime, all the coefficients corresponding to those  $a_{mi}$ ,  $a_{ni}$ ,  $a_{kj}$ ,  $a_{nj}$ ,  $a_{kl}$ , and  $a_{ml}$  in eqs (4-1)–(4-3) are set equal to zero.

In the case of larger molecules such as 1a-1j, the calculations involving larger basis sets such as 6-31G et al. are extremely costly. In this work, the complete FMO basis set and the various orbital interaction energies were constructed and calculated using the ab initio SCF-MO computation program at the STO-3G level. The various rotational geometries were optimized using AM1. It should be stressed that during the period of any ab initio SCF iteration, the geometries of a molecule, its fragments and fragment molecules were no longer optimized.

### **Results and Discussion**

**Geometry Optimization.** In our practical calculations, the rotational geometries of each of STB-type **1** were optimized using the various semiempirical calculations such as AM1, MNDO, MINDO/3, and PM3.<sup>12</sup> Our practical calculations and recent literature show that the AM1 method appears to be most suitable.<sup>3,21</sup> However, AM1 cannot treat correctly all the molecules. In fact, the abnormal difference in the twist angle  $\phi$  between the experiment and AM1 calculation occurs in molecule **1f**. According to the energy data in Table 2, it may result from its rather flat potential energy.

The starting geometry of each molecular conformation was taken from the crystal structure, and the geometry optimizations for the various rotational conformers were experimentally carried out under the following two models: (i) the full optimization (Model I); (ii) all the dihedral angles are kept to be  $0^{\circ}$  or  $180^{\circ}$ (Model II). In addition, the H and ring atoms in each of two aromatic rings were kept on same plane, and the twist angle  $\theta$ in a given rotational conformer was kept unchanged in above two models. Our practical calculations show that of all the dihedral angles, only the angle  $P-C_1-X-Z$  has the greatest effect on the preferential geometry, and a larger angle  $\theta$ corresponds generally to a larger deviation of the angle N<sub>7</sub>- $C_1-X-Z$  (X, Z = C, N) from 180° (see Figures 1-3). Therefore, the whole aromatic ring with a substituent group such as -NO<sub>2</sub>, -NH<sub>2</sub>, or -Cl can be considered approximately as a planar fragment, which will greatly simplify our computational procedure.

When  $\alpha \neq 0$  and  $\theta \neq 0$ , there should be eight types of the FMO interactions. However, the  $\sigma - \pi$  interaction results in the mixture of the  $\sigma$  and  $\pi$  FMOs and will not be considered here.

 $\pi$ -System Is Most Destabilized in the DPI State of Coplanar Geometry. According to the definitions of the Coulomb and exchange integral matrices J and K, we have the following theoretical expressions for the elements in eqs (3-1)-(3-3).<sup>22</sup>

$$F_{ij}^{(\pi)-\lambda} = H_{ij}^{(\pi)-\lambda} + \sum_{m} \sum_{n} D_{mn}^{(\pi)-\lambda} [(ij,mn) - 1/2(im,jn)]$$
(5-1)

$$F_{ik}^{(\pi)-\lambda} = H_{ik}^{(\pi)-\lambda} + \sum_{m} \sum_{n} D_{mn}^{(\pi)-\lambda} [(ik,mn) - 1/2(im,kn)] \quad (5-2)$$

$$F_{ik}^{(o)-\lambda} = H_{ik}^{(o)-\lambda} + \sum_{m} \sum_{n} D_{mn}^{(o)-\lambda} [(ik,mn) - 1/2(im,kn)]$$
(5-3)

The constrained conditions in the RHF<sup> $\pi$ </sup>-f and RHF<sup> $\pi$ </sup>-m ensure all the  $D_{mn}^{(\pi)-\sigma}$  and  $D_{mn}^{(o)-\sigma}$  ( $m \neq n$ ) are equal to zero except those between two pairs of the single occupied FMOs. In these cases, the effect of the  $\sigma$ -electron delocalization on the  $\pi$  system has been eliminated as far as possible.

In order to get deeper insight into the conjugation effect on the original energies  $E_{pq}^{(\alpha)-\pi}$ , the energy effect  $\Delta E_{\pi}^{(\pi)}(\theta)$  including its components  $\Delta E_{pq}^{(\pi)-\pi}(\theta)$  and  $\Delta E_{p}^{(\pi)-\pi}(\theta)$  were calculated (Tables 3 and 4). In accord with the classic viewpoint, the conjugation energy  $\Delta E_{ab+bc}^{(\pi)-\pi}(\theta)$  is most stabilizing at the coplanar geometry, and weakens with the rotation of fragment C about the C<sub>1</sub>-N<sub>7</sub> bond. The absolute value (|-1.1369|hartree) of  $\Delta E_{ab+bc}^{(\pi)-\pi}$  in the coplanar geometry is greatest of all the rotational geometries listed in Table 3, and its minimum value, about |-0.000 99|hartree, occurs in the vertical geometry with  $\alpha = \theta = 90^{\circ}$ . However, as shown by the data in Tables 3 and 4, the conjugation reduces, without exception, the original  $\pi$ energy  $E_{p}^{(n)-\pi}$  of each of fragments, and, moreover, the energy



Figure 5. The thermodynamic cycle for the orbital interactions and the definitions of the various energy differences. The numbers in parentheses are the values (hartrees) of the total electronic energies in four hypothetical states (FUL, DPI, DSI, and FUD) of the copolanar geometry of 1h.

TABLE 3: Energy Gain  $\Delta E_{pq}^{(\pi)-\pi}$ , Energy Losses  $\Delta E_p^{(\pi)-\pi}$ , Total  $\pi$  and  $\sigma$  Interaction Energies  $\Delta E_{\pi}^{(\pi)}$  and  $\Delta E_{\sigma}^{(\pi)}$ , and Total Electronic Energies  $E_{\pi}^{(\pi)}$  and  $E_{\sigma}^{(\pi)}$  in the DPI State of 1h, and Their Changes with the Rotation of Fragment C (Energy in Hartrees)

angle (	deg)									
θ	α	$\Delta E^{(\pi)-\pi}_{ab}$	$\Delta E_{bc}^{(\pi)-\pi}$	$\Delta E_a^{(\pi)-\pi}$	$\Delta E_b^{(\pi)-\pi}$	$\Delta E_c^{(\pi)-\pi}$	$\Delta E_{\pi}^{(\pi)}$	$\Delta E^{(\pi)}_{\sigma}$	$E_{\pi}^{(\pi)}$	$E^{(\pi)}_{\sigma}$
					Model II of C	Optimizing				
0	0	-0.54429	-0.592 56	0.550 15	0.433 80	0.242 19	0.088 67	-0.07647	-134.7154	-1167.2741
10	0	$-0.542\ 14$	-0.57464	0.549 37	0.420 35	0.234 03	0.086 63	-0.07458	-134.7285	-1167.3118
30	0	$-0.528\ 31$	-0.445 13	0.544 42	0.321 17	0.179 43	0.071 33	-0.06044	-134.8300	-1167.6070
50	0	-0.50427	$-0.248\ 88$	0.532 71	0.158 33	0.107 83	0.045 58	-0.036 63	-134.9147	-1167.6222
90	0	$-0.474\ 11$	-0.00068	0.516 63	-0.05451	0.023 01	0.010 34	-0.00335	-134.9125	-1167.0489
90	90	$-0.000\ 30$	-0.000 69	0.000 34	0.000 49	0.000 20	0.000 05	$-0.000\ 08$	-135.0351	-1167.1675
					Model I of C	Optimizing				
0		-0.54144	$-0.592\ 20$	0.547 48	0.432 71	0.242 36	0.088 54	-0.07636	-134.7147	-1167.2647
10		-0.53662	-0.57443	0.544 06	0.418 05	0.235 70	0.086 40	$-0.074\ 40$	-134.7296	-1167.3036
30		-0.52665	-0.45466	0.542 47	0.322 35	0.188 71	0.071 89	-0.061 03	-134.8072	-1167.4844
50		-0.50565	-0.271 93	0.532 61	0.172 14	0.121 31	0.048 31	$-0.039\ 10$	-134.8507	-1167.3113
90		$-0.473\ 32$	-0.002 91	0.516 33	-0.05607	0.025 67	0.009 68	-0.00273	-134.8104	-1166.4864

gain  $\Delta E_{ab+bc+ca}^{(\pi)-\pi}(\theta)$  is insufficient to compensate for the total energy loss  $\Delta E_{a+b+c}^{(\pi)-\pi}(\theta)$ . The total  $\pi$  energy effect  $\Delta E_{\pi}^{(\pi)}(\theta)$  is destabilizing. The  $\Delta E_{\pi}^{(\pi)}(0^{\circ})$  of **1h** is large up to 55.64 kcal/ mol. At the vertical geometry, there should be no  $\pi$  interactions between fragments except the long distance interaction between fragments A and C. The calculation results are  $\Delta E_{ab+bc}^{(\pi)-\pi} =$ -0.62 kcal/mol and  $\Delta E_{\pi}^{(\pi)} = 0.031$  kcal/mol (Table 3). As shown by the data of  $\Delta E_{\sigma}^{(\pi)}(\theta)$  in Tables 3 and 4, the  $\sigma$ 

As shown by the data of  $\Delta E_{\sigma}^{(\pi)}(\theta)$  in Tables 3 and 4, the  $\sigma$  framework is stabilized owing to the  $\sigma-\pi$  space interactions, while the  $\pi$  system itself is destabilized due to the  $\pi$ -electron interactions between fragments. However, this energy gain  $\Delta E_{\sigma}^{(\pi)}(\theta)$  is still insufficient to compensate for the  $\pi$  energy loss  $\Delta E_{\pi}^{(\pi)}(\theta)$ . The total energy effect  $\Delta E_{\pi}^{(\pi)}(\theta) + \Delta E_{\sigma}^{(\pi)}(\theta)$  is destabilizing. At the coplanar geometry of **1h**, for example, its value (7.66 kcal/mol) is greatest, and the total electronic energy (-1301.9895 hartrees) in the DPI state is the highest of four hypothetical electronic states (see Figure 5). It might be a reason why the symmetrization of the phenyl ring in **1h-VER** is better than that of **1h-R0** (Figure 3).

Destabilization of the  $\pi$ -System in the DPI State Is Due to  $\pi$ -Electron Delocalization. Electron delocalization is an important concept in modern organic chemistry. One problem is that "delocalization" is not directly measurable and there is no single definition underlying the use of this concept throughout chemistry.<sup>23</sup> As shown by Figure 6, the charge transfer (CT) mixes the occupied FMO of one fragment with the vacant FMO of the other and vice versa, and one of two exchange (EX) energies is associated with the interaction between the occupied FMOs. According to the Morokuma definitions,<sup>15</sup> these two interactions cause  $\pi$ -electron delocalization between fragments. Based on the PMO expression for two-electron interaction energy,<sup>24</sup> the CT energy  $\Sigma_{ov}^{pq}$  (Figure 6) can be defined as the energy gain of fragment P, and it is associated with the interaction which causes the delocalization of the  $\pi$ -electrons from P to Q. Comparison of the values of the  $\Sigma_p^2$  and the net  $\pi$ -electron charge  $D_{\rho}^{(\pi)}$  (Table 5) and inspection of their signs indicate that the quantity  $\Sigma_p^2$ , as defined by eqs (6-1)–(6-3), can be used to measure, indirectly, the net charge transfer.

$$\Sigma_a^2 = \Sigma_{ov}^{ba} - \Sigma_{ov}^{ab} \tag{6-1}$$

$$\Sigma_c^2 = \Sigma_{ov}^{bc} - \Sigma_{ov}^{cb} \tag{6-3}$$

$$\Sigma_b^2 = -(\Sigma_a^2 + \Sigma_c^2) \tag{6-2}$$

whether fragment P is a +M or -M group depends upon the sign of  $\Sigma_p^2$ . The signs of the  $D_a^{(\pi)}$  and  $\Sigma_a^2$  both are positive without exception; fragment A is +M group as far as twoelectron interaction is concerned. On the other hand, it is difficult to determine the contributions made by each of two

TABLE 4: Energy Gain  $\Delta E_{ab+bc}^{(\pi)-\pi}$ , Energy Losses  $\Delta E_p^{(\pi)-\pi}$ , CT Energy  $\Sigma_{ov}^{cb}$ , Total  $\pi$  and  $\sigma$  Interaction Energies  $\Delta E_{\pi}^{(\pi)}$  and  $\Delta E_{\sigma}^{(\pi)}$ , Total Electronic Energies  $E_{\pi}^{(\pi)}$  and  $E_{\sigma}^{(\pi)}$  in the DPI State of Stilbene-like Species, and the Changes with the Rotation of Fragment C (Energy in Hartrees)

angle	(deg)										
$\theta$	α	$\Delta E^{(\pi)-\pi}_{ab+bc}$	$\Delta E_a^{(\pi)-\pi}$	$\Delta E_b^{(\pi)-\pi}$	$\Delta E_c^{(\pi)-\pi}$	$\Sigma_{ov}^{cb_{a}}$	$\Delta E_{\pi}^{(\pi)}$	$\Delta E^{(\pi)}_{\sigma}$	$E_{\pi}^{(\pi)}$	$E^{(\pi)}_{\sigma}$	model
						Compound 1a					
0	0	-1.156 54	0.392 98	0.463 76	0.391 81	-0.469 82	0.091 47	-0.07724	-132.1603	-1131.6589	II
5	5	-1.14670	0.390 12	0.458 76	0.389 18	-0.46652	0.090 83	-0.07671	-132.1687	-1131.6866	Ι
20	20	-1.01044	0.351 21	0.390 41	0.350 51	-0.41928	0.081 69	$-0.068\ 87$	-132.2658	-1131.9565	Ι
						Compound 1i					
0	0	$-1.086\ 10$	0.370 63	0.443 10	0.359 74	-0.424 78	0.087 06	-0.07461	-134.5834	-1166.7678	II
5		-1.08124	0.370 70	0.440 27	0.357 19	-0.42171	0.086 61	-0.07422	-134.5856	-1166.7696	Ι
20		-1.01504	0.373 17	0.403 28	0.319 36	-0.37672	$0.080\ 48$	$-0.068\ 61$	-134.6308	-1166.9018	Ι
						Compound 1h					
0	0	-1.136 85	0.550 15	0.433 80	0.242 19	-0.40170	0.088 68	-0.07662	-134.7154	-1167.2741	II
5		-1.129 79	0.548 20	0.429 52	0.240 48	$-0.398\ 80$	0.088 06	-0.075~98	-134.7182	-1167.2761	Ι
						Compound 1f					
0	0	-1.18751	0.436 23	0.604 73	0.232 78	-0.39947	0.085 97	$-0.075\ 19$	-193.9805	-1588.3054	Π
5		-1.18236	0.435 96	0.601 38	0.230 87	-0.396 55	0.085 61	-0.07482	-193.9824	-1588.3087	Ι
20		-1.115 67	0.435 65	0.554 78	0.205 94	-0.35636	0.080 50	-0.069 99	-194.0056	-1588.3379	Ι
						Compound 1e					
0	0	-1.17891	0.538 06	0.547 58	0.180 87	-0.38201	0.087 32	-0.07622	-168.3976	-1754.1825	II
5		$-1.171\ 11$	0.534 28	0.544 25	0.179 57	-0.37847	0.086 74	-0.07576	-168.3997	-1754.1976	Ι
20		-1.104 93	0.530 53	0.495 18	0.160 74	-0.340 69	0.081 28	-0.07068	-168.4250	-1754.2161	Ι
						Compound 1g <sup>b</sup>					
0	0	-1.23637	0.823 43	0.431 83	0.056 22	-0.34569	0.074 71	-0.06445	-158.8848	-1292.3778	П
5		-1.23194	0.822 73	0.427 97	0.055 95	-0.34345	0.074 31	$-0.064\ 10$	-158.8863	-1292.3785	I
20		-1.163 73	0.812 81	0.369 94	0.049 61	-0.308 33	0.068 28	-0.058 35	-158.9106	-1292.4070	Ι
						Compound 1i					
0	0	-1 175 75	0 493 97	071634	0.048.37	-0.333.22	0.082.75	-0.072.86	-195 1525	-1605 7806	П
5	0	-1.170.04	0.492.91	0.711 34	0.048 27	-0.330.88	0.082.29	-0.072.37	-195.1525	-1605.7823	ī
20		-1.10563	0.488 24	0.649 97	0.044 36	-0.29789	0.076 76	-0.06737	-195.1867	-1605.8563	i
											-

<sup>*a*</sup> The energy effect  $\Sigma_{ov}^{cb}$  will be defined and used in the next section. <sup>*b*</sup> -N(Me)<sub>2</sub> group in **1g** has been replaced with a planar -NH<sub>2</sub>.



Figure 6. Morokuma's definitions of the FMO interactions between fragments P and Q (P, Q = A, B, C).

fragments to the EX energy  $\sum_{oo}^{pq}$ . Referring to the method for calculating the gross AO's charge,<sup>25</sup> the EX energy might be able to be divided evenly into two parts  $\sum_{oo}^{pq} = (1/2)\sum_{oo}^{pq} + (1/2)\sum_{oo}^{qp}$  (Table 5); still we cannot say which fragment is a -M group as far as the four-electron interaction is concerned.

A comparison of the data in Table 5 with the corresponding  $\Delta E_p^{(\pi)-\pi}(\theta)$  in Table 3 shows that the energy losses  $\Delta E_{b}^{(\pi)-\pi}(\theta)$  and  $\Delta E_{c}^{(\pi)-\pi}(\theta)$  become larger while the absolute values of the  $\Sigma_{ov}^{bc}(\theta) + \Sigma_{ov}^{ba}(\theta)$  and the  $\Sigma_{ov}^{cb}(\theta)$  increase with the geometry of 1h getting flatter. At the coplanar geometry, for example, the  $\Sigma_{ov}^{bc}(0^{\circ}) + \Sigma_{ov}^{ba}(0^{\circ})$  (-0.87472 hartree) and  $\Sigma_{av}^{cb}(0^{\circ})$  (-0.401 87) are most stabilizing, and the corresponding  $\Delta E_{b}^{(\pi)-\pi}(0^{\circ})$  (0.242 36) and  $\Delta E_{c}^{(\pi)-\pi}(0^{\circ})$  (0.432 71) both are most destabilizing. In Table 4, there are seven sets of the data listed in increasing order of the value of  $\Sigma_{ov}^{cb}(0^{\circ})$  in each of seven compounds. Table 4 shows further that from compound **1a** to **1i**, the value of the  $\Delta E_c^{(\pi)-\pi}(0^\circ)$  decreases as the absolute value of the  $\sum_{av}^{cb}(0^{\circ})$  decreases. In molecule **1a**, for example, the absolute value (|-0.4698| hartree) of the  $\Sigma_{ov}^{cb}(0^{\circ})$  and the value (0.3918 hartree) of the corresponding  $\Delta E_c^{(\pi)-\pi}(0^\circ)$  both are greatest, and the smallest values (|-0.3332| and 0.0484 hartree) of these two energies both occur in 1i. This comparison also indicates that in a given geometry with the  $\theta \neq 50^{\circ}$ , a larger energy loss  $\Delta E_p^{(\pi)-\pi}(\theta)$  corresponds to a larger value of the  $\Sigma_p^2(\theta)$ . In the  $\theta = 0^\circ$  geometry (Model I) of **1h**, for example, the value of the  $\sum_{p=0}^{2} (0^{\circ})$  decreases in the sequence:  $\Sigma_a^2(0^\circ) = 0.135\ 70\ \text{hartree} > \Sigma_b^2(0^\circ) = -0.017\ 46 > \Sigma_c^2(0^\circ) =$ -0.118 24, and the value of the corresponding  $\Delta E_p^{(\pi)-\pi}(0^\circ)$ decreases in the same sequence:  $\Delta E_a^{(\hat{\pi})-\pi}(0^\circ) = 0.54748$ hartree >  $\Delta E_b^{(\pi)-\pi}(0^\circ) = 0.432\ 71 > \Delta E_c^{(\pi)-\pi}(0^\circ) = 0.242\ 36.$ 

Every  $\pi$  system with  $\sum_{pq}^{ov}(\theta) < 0.0$  is destabilized (except  $\Delta E_b^{(\pi)-\pi}(90^\circ)$ ), and which one is most destabilized depends upon their values of  $\sum_{p}^{2}(\theta)$ .

TABLE 5: CT Energies  $\Sigma_{ov}^{pq}$ . Net CT Energies  $\Sigma_{p}^{2}$ , EX Energies  $\Sigma_{oo}^{pq}$  Occurring in Five Typical Geometries (Model I) of 1h, and the Net  $\pi$ -Electron Charge  $D_{p}^{(\pi)}$  on Each of Three Fragments (Energy in Hartrees)

	F				
	$\theta = 0^{\circ}$	$\theta = 10^{\circ}$	$\theta = 30^{\circ}$	$\theta = 50^{\circ}$	$\theta = 90^{\circ}$
		Fragme	nt A		
$\Sigma^{ab}_{av}$	-0.49032	-0.488 31	-0.495 35	$-0.500\ 18$	-0.503 93
$\Sigma_{a}^{2}$	0.135 70	0.136 46	0.147 20	0.160 95	0.180 64
$0.5\Sigma_{aa}^{ab}$	0.162 41	0.162 10	0.166 66	0.171 87	0.177 42
$D_a^{(\pi)}$	0.026 22	0.026 14	0.026 60	0.026 81	0.027 03
		Fragme	nt B		
$\Sigma_{av}^{ba} + \Sigma_{av}^{bc}$	-0.87472	-0.856 96	-0.74994	-0.58052	-0.325 57
$\Sigma_{h}^{2}$	-0.01746	-0.021 43	-0.052 91	-0.103 12	-0.18062
$0.5(\Sigma_{aa}^{ba}+\Sigma_{aa}^{bc})$	0.350 36	0.345 03	0.313 19	0.260 89	0.178 05
$D_b^{(\pi)}$	-0.013 49	-0.013 78	-0.016 43	-0.02058	$-0.027\ 12$
		Fragme	nt C		
$\Sigma_{av}^{cb}$	-0.401 87	-0.390 08	-0.30750	-0.183 46	$-0.002\ 27$
$\Sigma_c^{2^2}$	-0.118 24	-0.115 03	-0.09429	-0.05784	0.000 60
$0.5\Sigma_{aa}^{cb}$	0.187 95	0.182 93	0.146 53	0.089 02	0.000 63
$D_c^{(\pi)}$	-0.012 73	-0.012 36	$-0.010\ 17$	-0.006 23	0.000 09

TABLE 6: QMRE of 1h, Its  $\pi$  and  $\sigma$  Components  $\Delta E_{\pi}^{Q}$  and  $\Delta E_{\sigma}^{Q}$ , Total  $\pi$  and  $\sigma$  Electronic Energies  $E_{\pi}^{(\pi,\sigma)}$  and  $E_{\sigma}^{(\pi,\sigma)}$  in the FUD State, and Their Changes with the Rotation of Fragment C (Energy in Hartrees)

angle (	deg)					
θ	α	QMRE	$\Delta E^{ m Q}_{\pi}$	$\Delta E^{ m Q}_{\sigma}$	$E_{\pi}^{(\pi,\sigma)}$	$E^{(\pi,\sigma)}_{\sigma}$
0	0	0.008 44	-0.083 13	0.091 57	-134.661 80	-1167.965 79
350	0	0.008 23	-0.08498	0.093 21	-134.674 40	-1168.006 13
330	0	0.006 94	-0.099 35	0.106 29	-134.772 34	-1168.319 01
310	0	0.004 89	-0.125 24	0.130 13	$-134.854\ 25^{a}$	$-1168.357\ 51^{a}$
270	0	0.002 87	-0.161 32	0.164 19	-134.851 51	-1167.805 82

<sup>a</sup> Maximal absolute values.

TABLE 7: QMRE of Stilbene-like Species, and Their  $\pi$  and  $\sigma$  Components  $\Delta E_{\pi}^{Q}$  and  $\Delta E_{\sigma}^{Q}$  at the Planar Geometry (Hartrees)

compds	QMRE	$\Delta E^{ m Q}_{\pi}$	$\Delta E^{ m Q}_{\sigma}$
1a	0.014 10	0.009 27	0.004 83
1j	0.009 41	$-0.065\ 70$	0.075 11
1h	0.008 44	-0.083 13	0.091 57
1e	0.007 77	-0.04956	0.057 37
1f	0.007 70	-0.055 59	0.063 29
1i	0.006 84	-0.041 25	0.048 09
1g	0.006 30	-0.08324	0.089 54

The Quantum Mechanical Resonance Energy (QMRE) of Stilbene-like Species Is Destabilizing. According to the original definition,<sup>26</sup> the QMRE of a delocalized system in a given geometry of benzene is the difference between the energy of the true ground state and the energy of a single Kekule structure. In this work, it is defined as the difference in the electronic energy between the FUD and DSI states. As shown by Tables 6 and 7, the QMRE of each of STB-type 1 is destabilizing. The QMRE (0.008 44 hartree) of 1h, for example, is most destabilizing at its planar geometry (Table 6), and its value monotonically decreases with the rotation of fragment C. A comparison of the data in Table 7 with those in Table 4 and Table 1 shows that of all molecules listed in the tables, a larger QMRE (>0.008 hartree), such as those 0.0141, 0.0094, and 0.0084 hartree, respectively, in 1a, 1j, and 1h (Table 7) corresponds generally to a larger  $\sum_{ov}^{cb}(0^{\circ})$  and to a larger sum  $(\phi + \alpha > 35^{\circ})$  (Table 1).

It is known that benzene is strongly stabilized by the QMRE.<sup>27</sup> In order to make a comparison between the QMREs of benzene and molecules of type **1**, and to understand the role of the QMRE with regard to molecular geometry and chemical reactivity, the distortion of the benzene geometry, denoted as  $d_{SH}$ , is considered in this work, and the various energies

occurring in six typical  $d_{SH}$  geometries were calculated (Table 8). The  $d_{SH}$  distortion was previously investigated by Shaik and Hiberty.<sup>28</sup> The geometries  $d_{SH} \neq 0.0$  Å arise from variations in alternating CC bond lengths within the constraint that the contribution of the nuclear repulsion to the total energy remains constant, equal to that of the  $d_{SH} = 0.0$  Å geometry. The  $d_{SH}$ = 0.1644 Å geometry resembles an idealized cyclohexatriene structure of alternating single and double CC bond lengths  $R'_{cc}$  and  $R_{cc}$  (see Table 8). In our PMO calculation, a distorted benzene molecule was dissected into three ethylenic fragments A, B, and C. In each of three fragments, the length of the CC double bond was equal to that of the shorter  $R_{cc}$  in the composite system. Table 8 shows that the QMRE is most stabilizing at the  $d_{SH} = 0.0$  Å geometry and monotonically weakens as the carbon framework is increasingly distorted away from the  $d_{SH}$ = 0.0 Å. At the  $d_{SH}$  = 0.0 Å geometry, for example, the QMRE is -43.28 kcal/mol, and it is the average of the spectroscopy value<sup>29a</sup> (-50 kcal/mol) and that (-36 kcal/mol)<sup>29b</sup> suggested by thermochemical measures. However, the detail energy partition shows that the QMRE is a sum of two components  $\Delta E_{\sigma}^{Q} = E_{\sigma}^{(\pi,\sigma)} - E_{\sigma}^{(\sigma)}$  and  $\Delta E_{\pi}^{Q} = E_{\pi}^{(\pi,\sigma)} - E_{\pi}^{(\sigma)}$ . Whether the QMRE is stabilizing or destabilizing depends upon the response, expressed in terms of the  $\Delta E_{\alpha}^{Q}(d_{SH})$  and  $\Delta E_{\alpha}^{Q}(\theta)$ , respectively, of the  $\sigma$  frameworks to the delocalization of the  $\pi$ -electrons. In the case of STB-type 1,  $\Delta E_{\sigma}^{Q}(\theta)$  is always destabilizing and its value is slightly larger than the absolute value of the corresponding  $\Delta E_{\pi}^{Q}(\theta)$  which is generally stabilizing except for that in **1a**. Conversely, the  $\Delta E_{\sigma}^{Q}(d_{SH})$ , as shown by the data in Table 8, is always stabilizing, and the  $\Delta E_{\pi}^{Q}(d_{SH})$  is generally destabilizing except that in the  $d_{SH} = 0.0$  Å geometry of benzene. Particularly, the absolute value (|-0.0533|hartree) of the  $\Delta E_{\sigma}^{Q}(d_{SH} = 0.0)$  is about three time larger than that (|-0.0177| hartree) of the  $\Delta E_{\pi}^{Q}(0.0)$ . Therefore, it is the  $\sigma$ 

TABLE 8: QMRE (kcal/mol) of Benzene, Its Components  $\Delta E_{\pi}^{Q}$  and  $\Delta E_{\sigma}^{Q}$ , Electronic Energies  $E_{\pi}^{(\sigma)}$  and  $E_{\sigma}^{(\sigma)}$  in the DSI State, Those  $E_{\pi}^{(\pi,\sigma)}$  and  $E_{\sigma}^{(\pi,\sigma)}$  in the FUD State, and Their Changes along the  $d_{SH}$  Distortion (Energy in Hartrees except for QMRE)

$\pi$	$= -\theta$ $= = - = -$			m = (=	<b>5</b> 7	F · · · · · · · · · · · · · · · · · · ·
$d_{SH}(\text{\AA})$	0.0	0.0403	0.0811	0.1224	0.1644	0.2070
$R_{cc}$ (short)	1.40 Å	1.38	1.36	1.34	1.32	1.30
$R_{cc}$ (long)	1.40 Å	1.4203	1.4411	1.4624	1.4844	1.5070
QMRE	-43.281 875	$-31.083\ 080$	-20.865 963	-12.554 593	-5.868474	$-0.626\ 882$
$\Delta E_{\pi}^{\mathrm{Q}}$	-0.017645	0.001 388	0.015 810	0.026 050	0.0328 05	0.036 767
$\Delta E_{\sigma}^{\ddot{Q}}$	-0.051 329	$-0.050\ 922$	$-0.049\ 062$	$-0.046\ 057$	$-0.042\ 157$	-0.037766
$E_{\pi}^{(\sigma)}$	-39.744 438	-39.765 388	-39.786 453	-39.807 735	-39.827 721	-39.847 374
$E_{\sigma}^{(\sigma)}$	-391.040 527	-391.036 011	-391.029 022	-391.020 599	-391.001 709	$-390.978\ 485$
$E_{\pi}^{(\pi,\sigma)}$	-39.762 085	-39.764 000	-39.770 645	-39.781 689	-39.794 918	-39.810 608
$E_{\sigma}^{(\pi,\sigma)}$	-391.091 858	-391.086 914	-391.078 094	-391.066 681	-391.043 884	-391.016 266
0						

TABLE 9: Occupied  $\pi$  MOs and Energy Changes along the  $d_{SH}$  Distortion (Energy in Hartrees)<sup>*a*</sup>

-		0. 0				
$d_{SH}({ m \AA})$	0.0	0.0403	0.0811	0.1224	0.1644	0.2070
21st (HOMO)	-0.331 63	-0.335 56	DSI State -0.339 77	-0.344 28	-0.349 04	-0.354 10
21st (HOMO) 17th	-0.278 24 -0.453 21	-0.279 02 -0.453 21	FUD State -0.281 37 -0.453 27	$-0.285\ 13$ $-0.453\ 44$	-0.290 10 -0.453 75	-0.296 09 -0.454 29

<sup>*a*</sup> In the DSI state, three occupied  $\pi$  MOs, 21st, 20th, and 19th, are degenerate. There are doubly degenerate levels, 21st and 20th, in the FUD state.

TABLE 10: Total Electronic Energy  $E_e$ , Nuclear Repulsion  $E_v$ , Total Molecular Energy  $E^T$ , Potential Energies  $RE_{\pi}^{(\sigma)}$  and  $RE_{\sigma}^{(\sigma)}$ , and Electronic Energies  $E_{\pi}^{(\sigma)}$  and  $E_{\sigma}^{(\sigma)}$  in the DSI State of Five Typical Geometries of 1h (Energy in Hartrees)

$\theta$ (deg)	$RE_{\pi}^{(\pi)}$	$RE_{\sigma}^{(\sigma)}$	$E_{\pi}^{(\sigma)}$	$E^{(\sigma)}_{\sigma}$	$E_{ m e}$	<i>RE</i> <sub>e</sub>	$E_v$	$E^{\mathrm{T}}$
				Model I of Optimi	izing			
$0^a$	0.0000	0.0000	-134.5778	-1168.0484	-1302.6175	0.0000	740.5334	-562.0842
350	-0.0149	-0.0434	-134.5902	-1168.0918	-1302.6718	-0.0543	740.5874	-562.0844
330	-0.0827	-0.2531	-134.6510	-1168.3015	-1302.9333	-0.3158	740.8477	-562.0855
310	-0.1360	-0.1243	-134.6682	-1168.1727	-1302.8076	-0.1901	740.7220	-562.0856
270	-0.0957	0.6393	-134.5876	-1167.4091	-1301.9436	0.6739	739.8610	-562.0826

<sup>*a*</sup> The referential geometry for the calculations of the potential energies. The energies  $E_v$ ,  $E_e$ , and  $E^T$  were obtained from full SCF computation at the STO-3G level.

framework for the  $d_{SH} = 0.0$  Å geometry to be strongly stabilized by the QMRE. Benzene is  $\sigma$  aromatic.<sup>30</sup> On the other hand, the  $\pi$  potential energy  $RE_{\pi}^{(\pi,\sigma)}(0.0) = E_{\pi}^{(\pi,\sigma)}(0.0) - E_{\pi}^{(\pi,\sigma)}(0.1644)$  is large, up to 20.6 kcal/mol (Table 8), revealing that the  $\pi$ -system of benzene is destabilized, and it prefers a distorted geometry.<sup>31</sup>

In the DSI state of benzene, the differences  $dE_{\sigma}^{(\sigma)}(d_{SH}) = E_{\sigma}^{(\sigma)}(d_{SH}) - E_{\sigma}^{(\sigma)}(d_{SH}^{\circ}) < 0.0, \ dE_{\pi}^{(\sigma)}(d_{SH}) = E_{\pi}^{(\sigma)}(d_{SH}) - E_{\sigma}^{(\sigma)}(d_{SH}^{\circ}) > 0.0$  when  $d_{SH} < d_{SH}^{\circ}$ , and the absolute value of the  $dE_{\sigma}^{(\sigma)}(d_{SH})$  is less than that of the  $dE_{\pi}^{(\sigma)}(d_{SH})$ . The  $dE_{\sigma}^{(\sigma)}(d_{SH})$  between the  $d_{SH} = 0.0$  and 0.1644 Å geometries is, for example, -24.359 kcal/mol, and the corresponding  $dE_{\pi}^{(\sigma)}(d_{SH})$  is large up to 52.261 kcal/mol. The  $\sigma$ -framework in the DSI state only possesses a distortive tendency. It is the  $\pi$  delocalization to make this tendency become an effective driving force, expressed in terms of the  $dE_{\sigma}^{(\pi,\sigma)}(d_{SH}) = [E_{\sigma}^{(\pi,\sigma)}(d_{SH}) - E_{\sigma}^{(\pi,\sigma)}(d_{SH})]$  whose absolute value is now larger than that of the  $dE_{\pi}^{(\pi,\sigma)}(d_{SH}) = E_{\pi}^{(\pi,\sigma)}(d_{SH}) - E_{\pi}^{(\pi,\sigma)}(d_{SH})$ , for distorting the  $d_{SH} \neq 0.0$  Å toward the symmetrical geometry.<sup>31</sup> The  $dE_{\sigma}^{(\pi,\sigma)}(d_{SH} = 0.0)$  between the  $d_{SH} = 0.0$  and 0.1644 Å geometries is, for example, -30.104 kcal/mol, and the corresponding  $dE_{\pi}^{(\pi,\sigma)}(0.0) = 20.603$  kcal/mol.

Table 9 shows further that in a given  $d_{SH}$  geometry, the energy of the highest occupied MO (HOMO) of the  $\pi$  type in the FUD state is always higher than that in the DSI state. Along the  $d_{SH}$ distortion, the energy, about -0.278 24 hartree, of the HOMO is highest at the  $d_{SH} = 0.0$  Å geometry. This energy character, together with those indicated by the  $E_{\pi}^{(\pi,\sigma)}(d_{SH})$  in Table 8 and the  $E_{\pi}^{(\pi,\sigma)}(\theta)$  in Table 6, is in accordance with the chemical feature that the  $\pi$  systems of benzene and STB-type **1** both are reactive toward electronphilic attack. However, the high stability of benzene due to the  $\Delta E_{\sigma}^Q(0.0) < 0.0$  (-32.21 kcal/mol) is getting weaker while its  $\pi$ -system is increasingly localized under the electrophile attacking. In the transition state, the  $\sigma$ -framework of benzene is reluctant to undergo addition reaction and has to opt for "aromatic" substitution instead in order to maintain its original  $\sigma$ -aromaticity. On the other hand, STB-type **1** are willing to undergo addition reaction owing to their  $\Delta E_{\sigma}^Q(\theta) > 0.0$ . During the period of preparing **1**, we found that the -CH=N- double bond is very unstable in its alcohol solution; the addition product is 2-ethoxyl-2-(4-nitrophenyl)-N-(2-pyrimidyl)ethylamine.

*σ* Interaction Is a Main Driving Force for Out-of-Plane Twist. The electronic energy of the DSI state is the lowest of four hypothetical states. In this state, all the elements, such as  $F_{ij}^{(\sigma)-\pi}$ ,  $H_{ij}^{(\sigma)-\pi}$ , and  $D_{ij}^{(\sigma)-\pi}$  ( $i \neq j$ ) corresponding to those in eqs (3-1)-(3-2), are equal to zero. Therefore, the potential energy, denoted as  $RE_{\sigma}^{(\sigma)}(\theta) = E_{\sigma}^{(\sigma)}(\theta) - E_{\sigma}^{(\sigma)}(0^{\circ})$ , is useful for analyzing the molecular conformation. In the region of the θ from 0 to about 40°, the absolute values of the various energies in **1h**, such as the  $E_{\sigma}^{(\sigma)}(\theta)$ ,  $E_{e}(\theta)$  (Table 10), and  $E_{\pi}^{(\pi)}(\theta)$  (Table 3), increase concurrently as the nuclear repulsion  $E_v$  (Table 10) becomes larger. In a given conformer, the absolute value of  $RE_{\sigma}^{(\sigma)}(\theta)$  is generally three times larger than that of the  $RE_{\pi}^{(\sigma)}(\theta)$ , and it is very close to that of the  $RE_{e}(\theta)$ . The

TABLE 11: Total  $\sigma$ -Electronic Energy  $E_{\sigma}^{(\sigma)}$  in the DSI States, Net  $\sigma$ -Electron Charge  $D_{c}^{(\sigma)}$  and the Ratio, de/dv, of the  $dE_{\sigma}^{(\sigma)}$  to  $dE_{v}$  (Energy in Hartrees)

$\theta$ (deg)	$E^{(\sigma)}_{\sigma}$	$D_c^{(\sigma)}$	de/dv
	1h		
0	-1168.0484	0.109 37	
5	-1168.0606	0.109 51	-0.82
	1i		
0	-1606.5901	0.091 59	
5	-1606.5965	0.091 74	-0.80
	1g		
0	-1293.1949	0.101 49	
5	-1293.1985	0.101 58	-0.78
	1j		
0	-1167.5517	0.125 02	
5	-1167.5543	0.125 15	-0.82
	1f		
0	-1589.1171	0.112 83	
5	-1589.1206	0.112 95	-0.74
	1e		
0	-1754.9791	0.109 45	
5	-1754.9830	0.109 56	-0.69

 $RE_{\sigma}^{(\sigma)}$  plays a predominant role in determining the preferential geometry of **1h**.

In flexible molecules such as STB-type **1**, it is difficult to determine which pair of the atoms makes the greatest contribution to the driving force. According to the definition  $E_v = \sum_i \sum_{j-1} (e_i e_j / r_{ij})$ ,  $E_v$  can be, indirectly, used to characterize the interaction distance between fragments, and the quantity de/dv in eq 7 can be defined as a generalized driving force for the out-of-plane twist.

$$de/dv = [E_{\sigma}^{(\sigma)}(5^{\circ}) - E_{\sigma}^{(\sigma)}(0^{\circ})]/[E_{v}(5^{\circ}) - E_{v}(0^{\circ})]$$
(7)

Comparison of the values of de/dv in Table 11 and those of the angle  $\phi$  in Table 1 shows that a larger absolute value (>0.80) of the de/dv corresponds to a larger twist angles  $\phi$  (>30°). The calculations for the net  $\sigma$  electronic charge  $D_c^{(\sigma)}(\theta)$  of fragment C (Table 11) show that, in the three typical molecules, the values of the  $dD_c^{(\sigma)} = D_c^{(\sigma)}(5^\circ) - D_c^{(\sigma)}(0^\circ)$  are in the sequence:  $1.5 \times 10^{-4}$  (**1i** with a -NO<sub>2</sub> group and two ring-nitrogen atoms) > 1.4  $\times 10^{-4}$  (**1h** with a ring-nitrogen atom on fragment C) >  $1.3 \times 10^{-4}$  (**1j** with a ring-nitrogen atom on fragment A), and their respective values of the angle  $\phi$  are 50 (**1i**) > 38 (**1h**) > 35° (**1j**). It seems that the electron-withdrawing (-I) groups and the ring-nitrogen atoms have an obvious influence upon the twist angle.

#### Summary

We have been successful in separating  $\sigma$  from  $\pi$  FMOs based on our new procedure. Besides the well-known resonance interaction between fragments, the  $\sigma$ -electron interaction, arising from the effect of the  $\pi$ -electron delocalization on the  $\sigma - \pi$  space interactions, is also stabilization. However, the delocalization of the  $\pi$ -electrons in the DPI state not only reduces the original  $\pi$  energies in fragments, but also the energy gains are insufficient to compensate for the energy loss. The  $\pi$ -electron delocalization in the DPI state is found to be destabilization. As a result, the DPI state is most destabilized at a coplanar geometry, and, in a given geometry, its electronic energy is highest of four hypothetical states. The characteristic of the QMRE depends upon the response of the  $\sigma$  framework to the  $\pi$  delocalization. In the case of stilbene-like species, the QMRE is destabilizing. On the other hand, the QMRE of benzene is stabilizing. However, it is the  $\sigma$  framework, rather than the  $\pi$  system itself, which is strongly stabilized by the QMRE, revealing that benzene is  $\sigma$  aromatic.

Contrary to the viewpoints in the literature, the driving forces for the out-of-plane twist of stilbene-like species are due to the  $\sigma$  orbital interaction and the QMRE. It seems that the electronwithdrawing (-I) groups on the aromatic ring and the ringnitrogen atoms, has an obvious influence on the twist angle.

# **Experimental Section**

**General Methods.** All starting materials were obtained commercially as reagent grade. Melting points were determined on a Nagoya apparatus and are uncollected. <sup>1</sup>H NMR spectra were recorded on a Varian Unity 200 NMR spectrometer. Crystal structures of molecules were determined by a Nicolet R3WE X-ray diffractometer. The crystal data of each of the following eight compounds are listed in Table 12.

*N*-(4-Chlorophenyl)methylene-2-pyridineamine (1e) was prepared from 4-chlorobenzaldehyde and 2-pyridineamine:<sup>32</sup> mp 96–99 °C; <sup>1</sup>H NMR (CDCl<sub>3</sub>) 9.12 (s, 1H), 8.56 (d, 1H), 7.18–7.92 (m, 7H).

*N*-(4-Nitrophenyl)methylene-2-pyridineamine (1f) was prepared from 4-nitrobenzaldehyde and *N*-(triphenylphosphoranylidene)-2-pyridineamine:<sup>32</sup> mp 147–148 °C; <sup>1</sup>H NMR (CDCl<sub>3</sub>) 9.27 (s, 1H), 8.58 (d, 1H), 8.38–7.25 (m, 7H).

*N*-(4-*N*,*N*-Dimethylaminophenyl)methylene-2-pyridineamine (1g) was prepared from 4-*N*,*N*-dimethylbenzaldehyde and 2-pyridineamine:<sup>32</sup> mp 123–124 °C; <sup>1</sup>H NMR (CDCl<sub>3</sub>) 9.1 (s, 1H), 8.50 (d, 1H), 7.9–6.8 (m, 7H), 3.2 (s, 6H).

*N*-(4-Nitrophenyl)methylene-2-pyrimidineamine (1i) was prepared from 4-nitrobenzaldehyde and *N*-(triphenylphospho-

TABLE 12:	Crystal Data of	Four Stilbene-like	Molecules 1 and Four	Ketenimine Derivatives 2 <sup><i>a</i></sup>
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	1e	1f	1g	1i	2a	2b	2c	2d
formula	C <sub>12</sub> H <sub>9</sub> ClN <sub>2</sub>	$C_{12}H_9N_3O_2$	$C_{14}H_{15}N_3$	$C_{11}H_8N_4O_2$	C <sub>20</sub> H <sub>15</sub> N	$C_{20}H_{14}N_2O_2$	$C_{22}H_{18}N_2O_4$	$C_{22}H_{20}N_2$
fw	216.66	227.220	225.290	228.210	269.00	314.330	374.380	312.400
color	colorless	yellow	yellow	yellow	yellow	red		yellow
a	6.509	7.096	11.923	6.015	20.594	7.972	13.439	9.919
b	8.005	28.754	17.914	13.393	8.753	18.951	9.429	12.838
с	20.383	10.969	12.059	25.572	17.471	11.062	15.099	14.010
α	90.000	90.000	90.000	90.000	90.000	90.000	90.000	90.000
β	98.270	106.500	103.990	90.000	101.698	106.911	93.171	90.000
γ	90.000	90.000	90.000	90.000	90.000	90.000	90.000	90.000
U	1051.000	2145.9	2499.300	2060.100	3083.900	1598.900	1910.400	1785.000
$D_{\rm x}$	1.369	1.407	1.197	1.472	1.158	1.306	1.302	1.162
Ζ	4	8	8	8	8	4	4	4
absorp coeff	0.328	0.100	0.073	0.107		0.086	0.091	0.064
space group	$P2_{1}/n$	$P2_1$	$P2_{1}/c$	$Pca2_1$	C2/c	$P2_{1}/n$	$P2_{1}/n$	$P2_{1}2_{1}2_{1}$

<sup>*a*</sup> Units:  $\alpha$ ,  $\beta$ , and  $\gamma$ , deg; U, Å<sup>3</sup>;  $D_x$ , g/cm<sup>3</sup>; absorption coefficient, cm<sup>-1</sup>.

ranylidene)-2-pyrimidineamine:<sup>32</sup> mp 236–238 °C; <sup>1</sup>H NMR (CDCl<sub>3</sub>) 9.33 (s, H), 8.84 (d, 2H), 7.29–8.40 (m, 6H).

*N*-(**Diphenylethenylidene**)**benzeneamine** (**2a**) was obtained as bright yellow crystalline from phenyl isocyanate and (diphenylmethylene)triphenylphosphorane:<sup>33</sup> mp 55–56 °C; <sup>1</sup>H NMR (CDCl<sub>3</sub>) 7.32–7.40 (m, Ar-H).

*N*-(**Diphenylethenylidene**)-4-nitrobenzeneamine (2b) was obtained as a red crystal from triphenylphosphine, bromine, triethylamine, and *N*-(4-nitrophenyl)diphenylacetamide:<sup>34</sup> mp 84–86 °C; <sup>1</sup>H NMR (CDCl<sub>3</sub>) 8.27 (d, 2H), 7.45 (d, 2H), 7.28–7.40 (m, 10H).

*N*-(**Bis**(4-methoxyphenyl)ethenylidene)-4-nitrobenzeneamine (2c) was obtained using the same procedure for preparing 2a. It was obtained as red crystals: mp 103.5–105.5 °C; <sup>1</sup>H NMR (CDCl<sub>3</sub>) 6.92, 7.24 (2d, 8H), 7.44, 8.26 (2d, 4H), 3.82 (s, 6H).

*N*-(Diphenylethenylidene)-4-(*N*,*N*-dimethylamino)benzeneamine (2d) was obtained using the same procedure for preparing 2a. It was obtained as yellow crystals: mp 90–92 °C; <sup>1</sup>H NMR (CDCl<sub>3</sub>) 6.69 (d, 2H), 7.20–7.36 (12H, m), 2.98 (s, 6H).

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